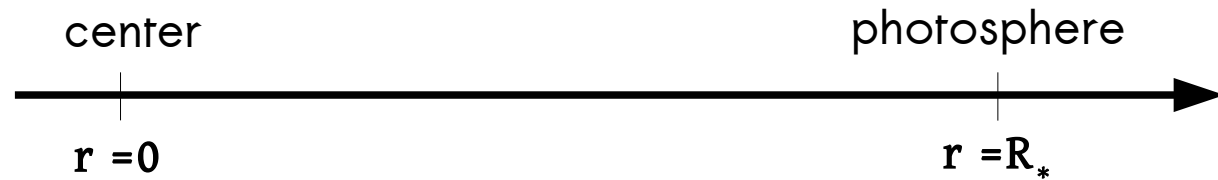
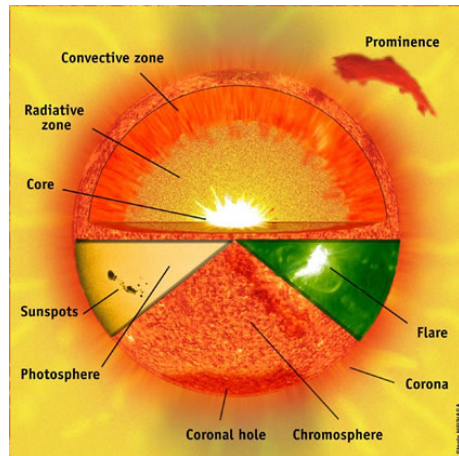
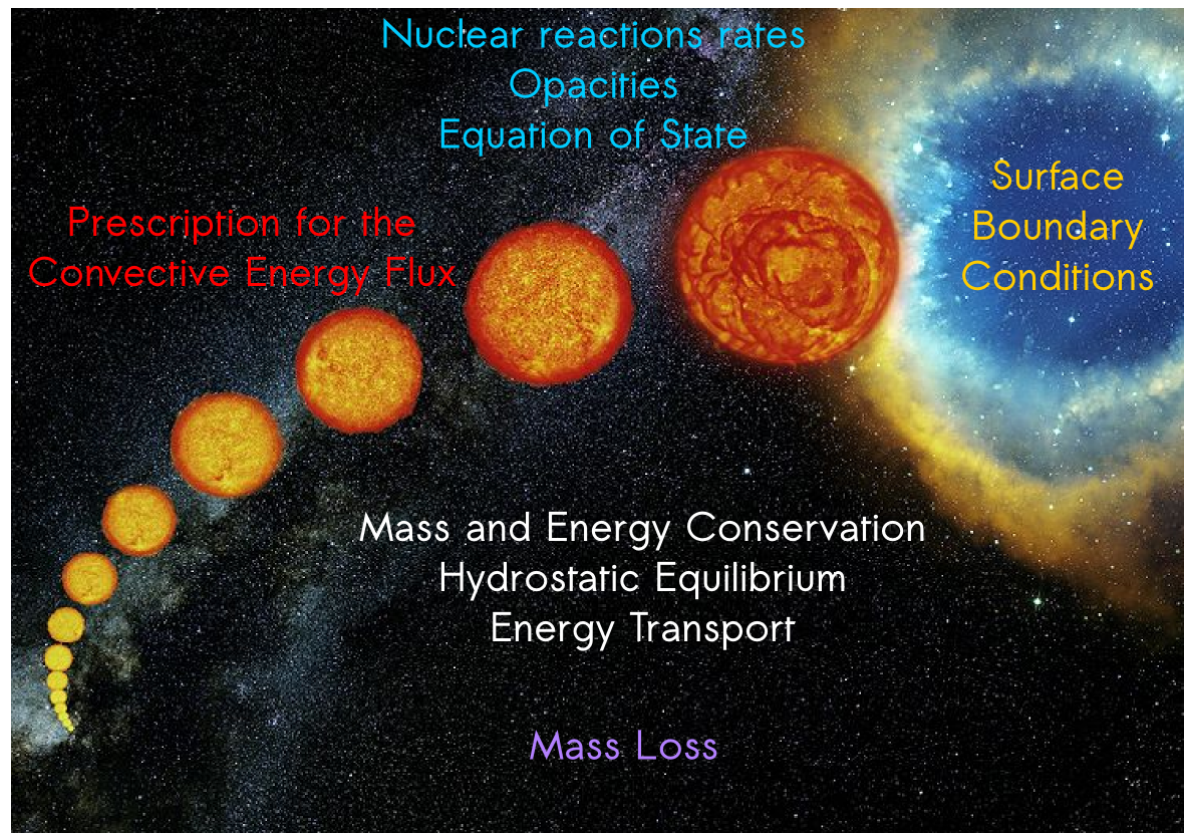


# Basic Assumptions for Stellar Evolution Models

From the complex to the “simple” picture : spherical symmetry applied



Initial mass  
and  
chemical composition



# Stellar structure and evolution equations

space coordinate

time coordinate

$$\frac{\partial}{\partial m} = \frac{\partial r}{\partial m} \frac{\partial}{\partial r} \quad \frac{\partial}{\partial t} \Big|_m = \frac{\partial}{\partial t} \Big|_r + \underbrace{\frac{\partial r}{\partial t} \Big|_m}_{v(r)} \frac{\partial}{\partial r} = \frac{D}{Dt}$$

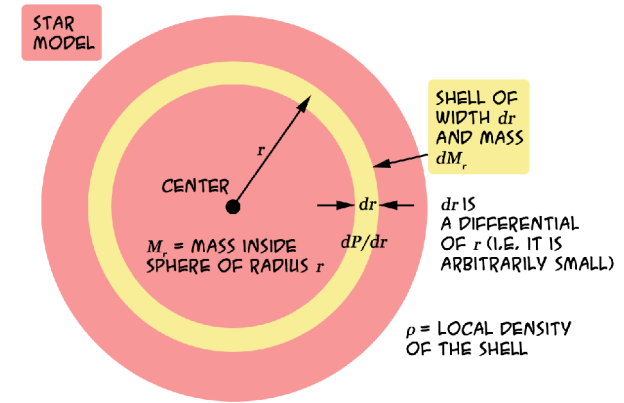
$$\frac{\partial r}{\partial m} = \frac{1}{4\pi r^2 \rho}$$

$$\frac{\partial P}{\partial m} = -\frac{1}{4\pi r^2} \left( \frac{Dv}{Dt} + \frac{\partial \Phi}{\partial m} \right) = -\frac{1}{4\pi r^2} \left( \frac{Dv}{Dt} + \frac{Gm}{r^2} \right)$$

$$\frac{\partial L}{\partial m} = \epsilon_n - \epsilon_\nu - C_p \frac{\partial T}{\partial t} + \frac{\delta}{\rho} \frac{\partial P}{\partial t} = \epsilon_n - \epsilon_\nu + \epsilon_g$$

$$\frac{\partial T}{\partial m} = -\frac{GmT}{4\pi r^4 P} \frac{d \ln T}{d \ln P} \Big|_{\text{medium}} = -\frac{GmT}{4\pi r^4 P} \nabla$$

$$\frac{\partial X_i}{\partial t} = \frac{m_i}{\rho} \left( \sum_j r_{ji} - \sum_k r_{ik} \right) \quad \forall i$$



## Associated boundary conditions

$$@ \quad m = 0 \quad r(m = 0, t) = 0 \quad L(m = 0, t) = 0$$

$$@ \quad m = M_* \quad T(m = M_*, t) = T_{\text{phot}} \quad \rho(m = M_*, t) = \rho_{\text{phot}}$$

if the surface is in radiative equilibrium

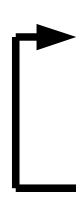
$$m = M_* \quad T(m = M_*, t) \approx 0 \quad \rho(m = M_*, t) \approx 0$$

# Characteristic timescales of stellar evolution

$$t_{\text{dyn}} \ll t_{\text{therm}} \ll t_{\text{nuc}}$$

→ rates of nuclear processes determine stellar evolution

→ can decouple equation for chemical composition from the others

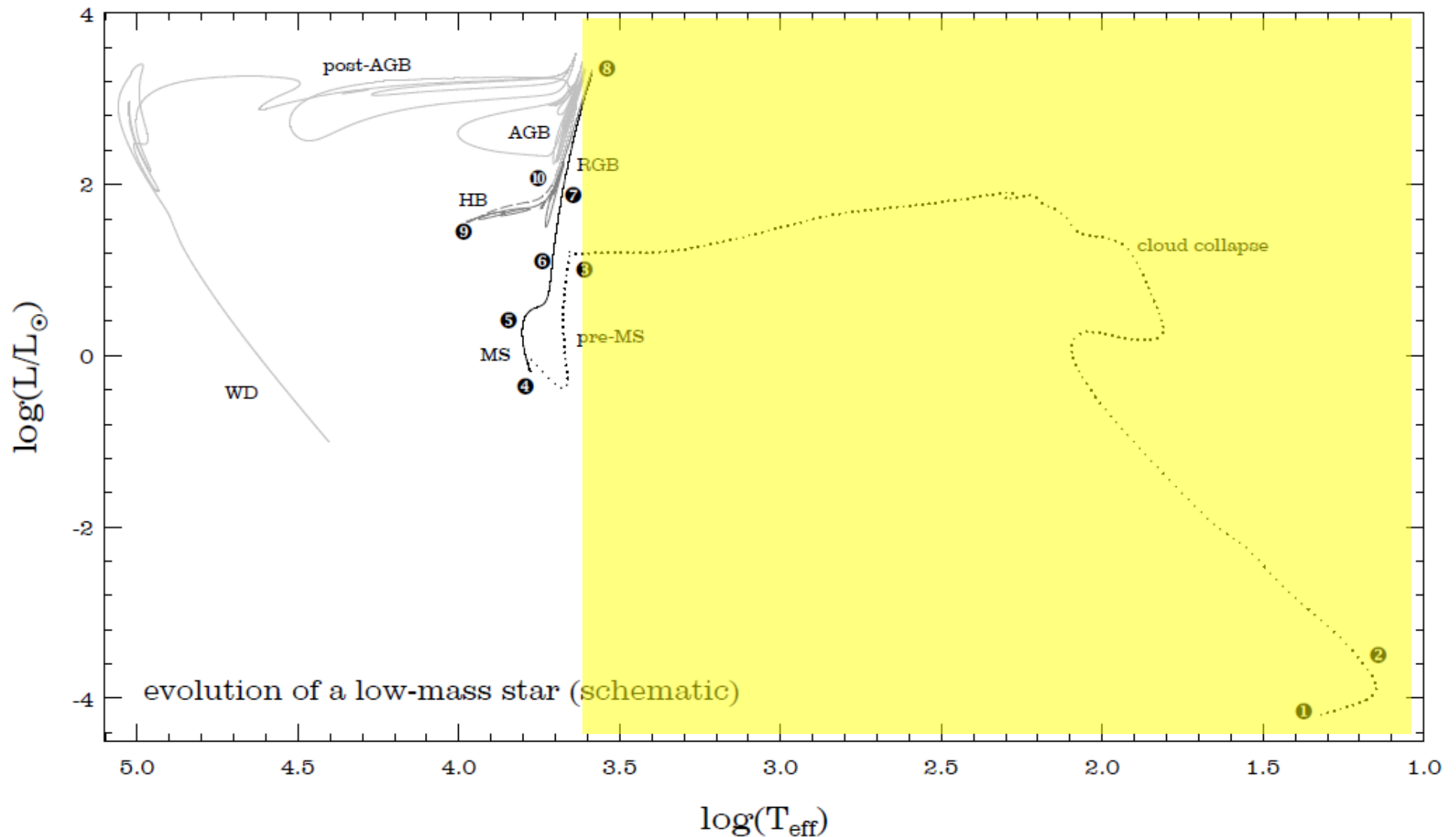
- 
1. Solve stellar structure equations for given composition
  2. Apply time step and determine new composition

# Solving stellar structure equations

- Four differential equations with boundary conditions at
  - \* center of star ( $m = 0$ ):  $r = 0$ ,  $L = 0$
  - \* surface of star ( $m = M$ ): fit interior solution to a stellar atmosphere model
- Three "material functions" (for  $\rho$ ,  $\kappa$ ,  $q$ )
- Input parameters:  
mass  $M$ , chemical composition  $X(t)$ ,  $Y(t)$ ,  $Z(t)$
- Output:  $r(m)$ ,  $P(m)$ ,  $L(m)$ ,  $T(m)$ ,  $\rho(m)$ ,  $\kappa(m)$ ,  $q(m)$ , for each time  $t$ ,  
in particular  $T_{\text{eff}}$ ,  $L$ ,  $R$ ,  $\rho_c$ ,  $P_c$
- Equations are highly non-linear and coupled  $\rightarrow$  have to be solved with numerical methods



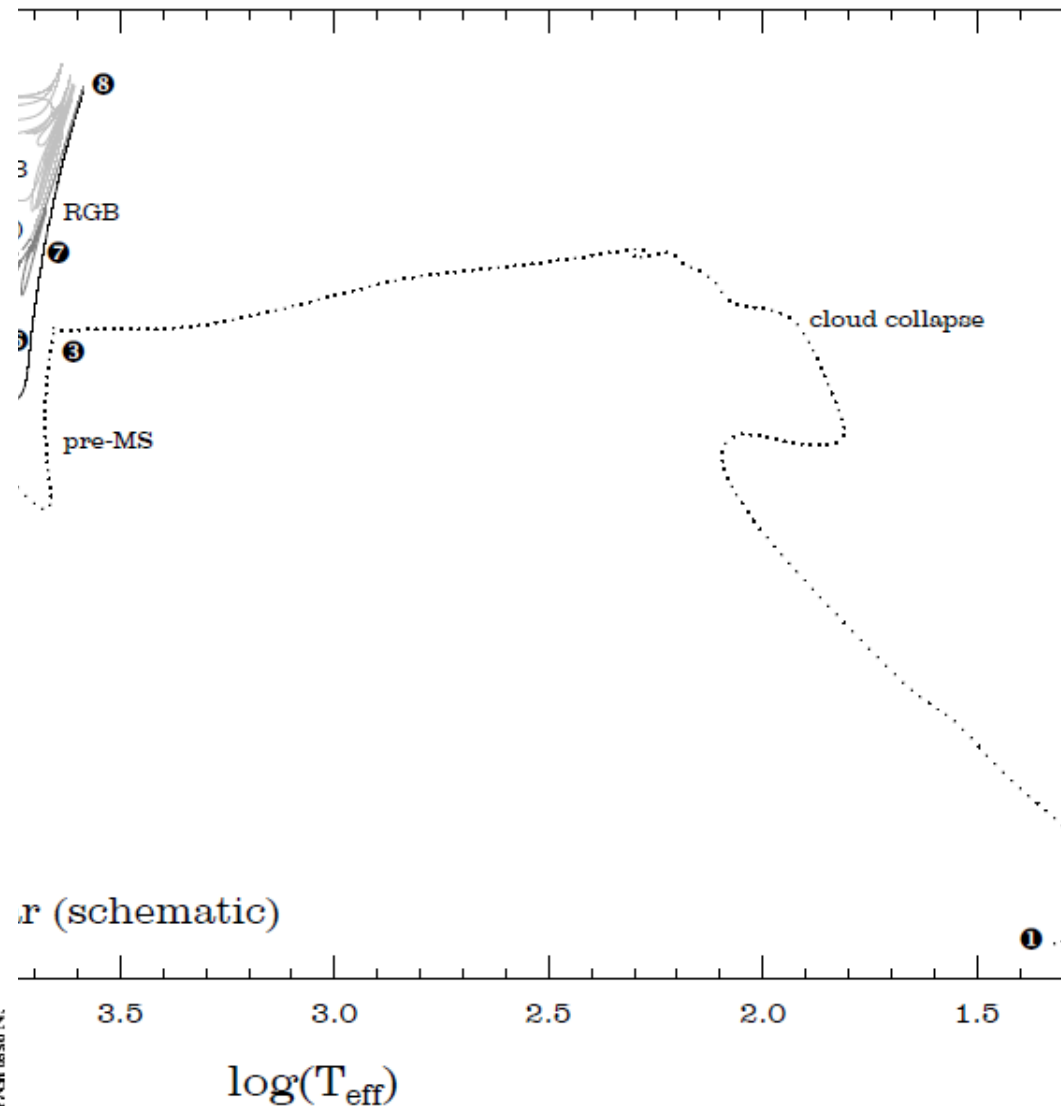
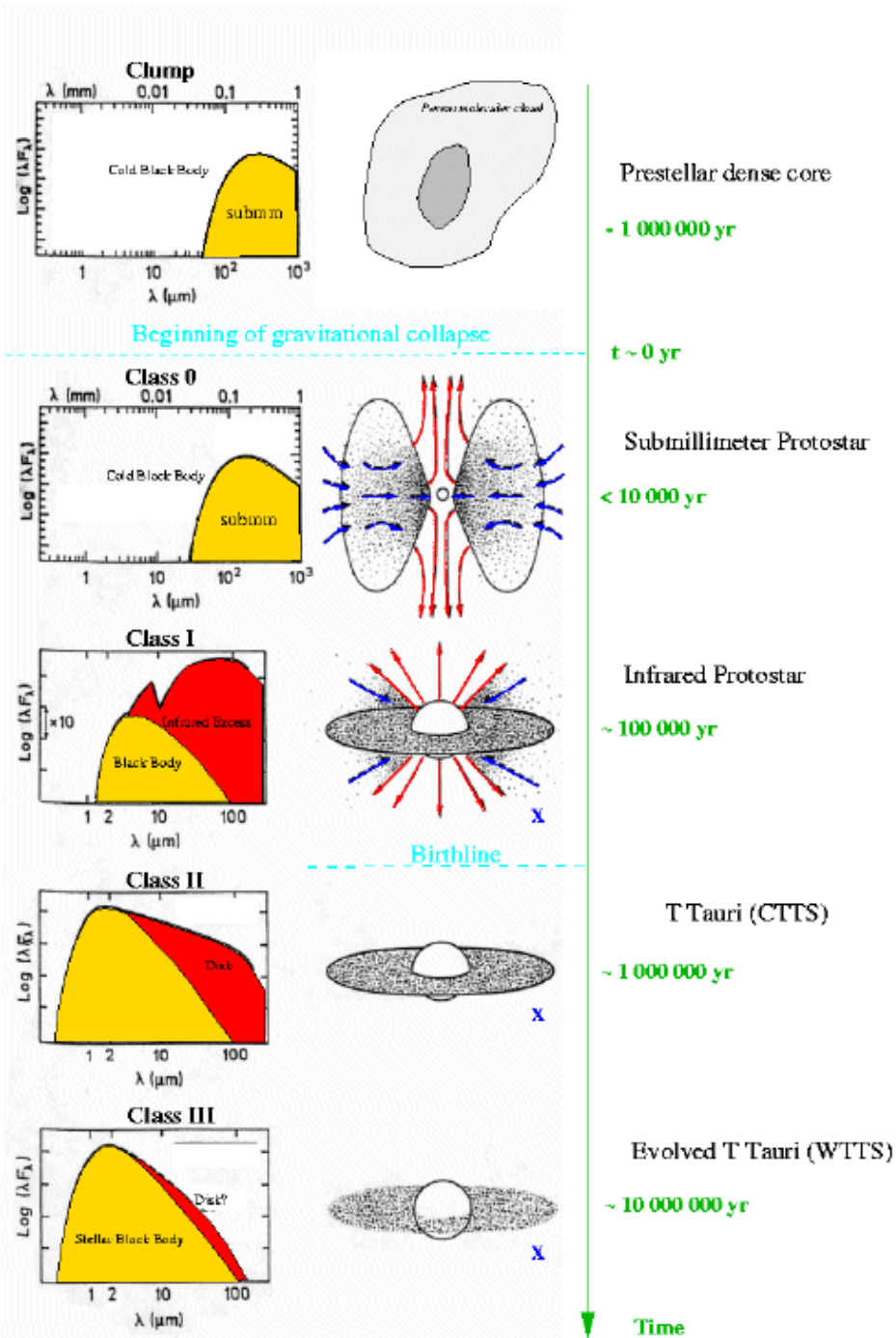
# Pre-stellar evolution



# Infrared/Submillimeter Young Stellar Object Classification

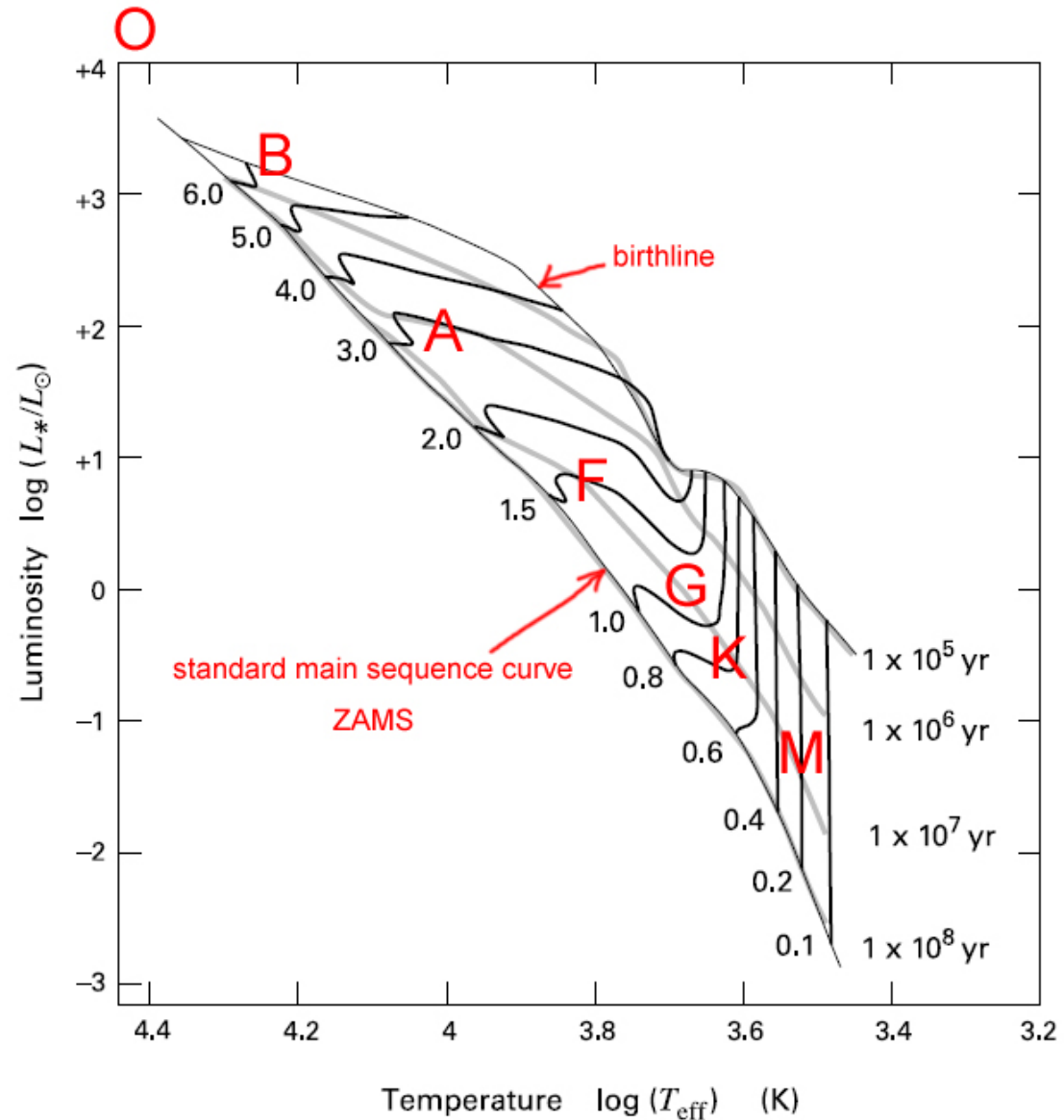
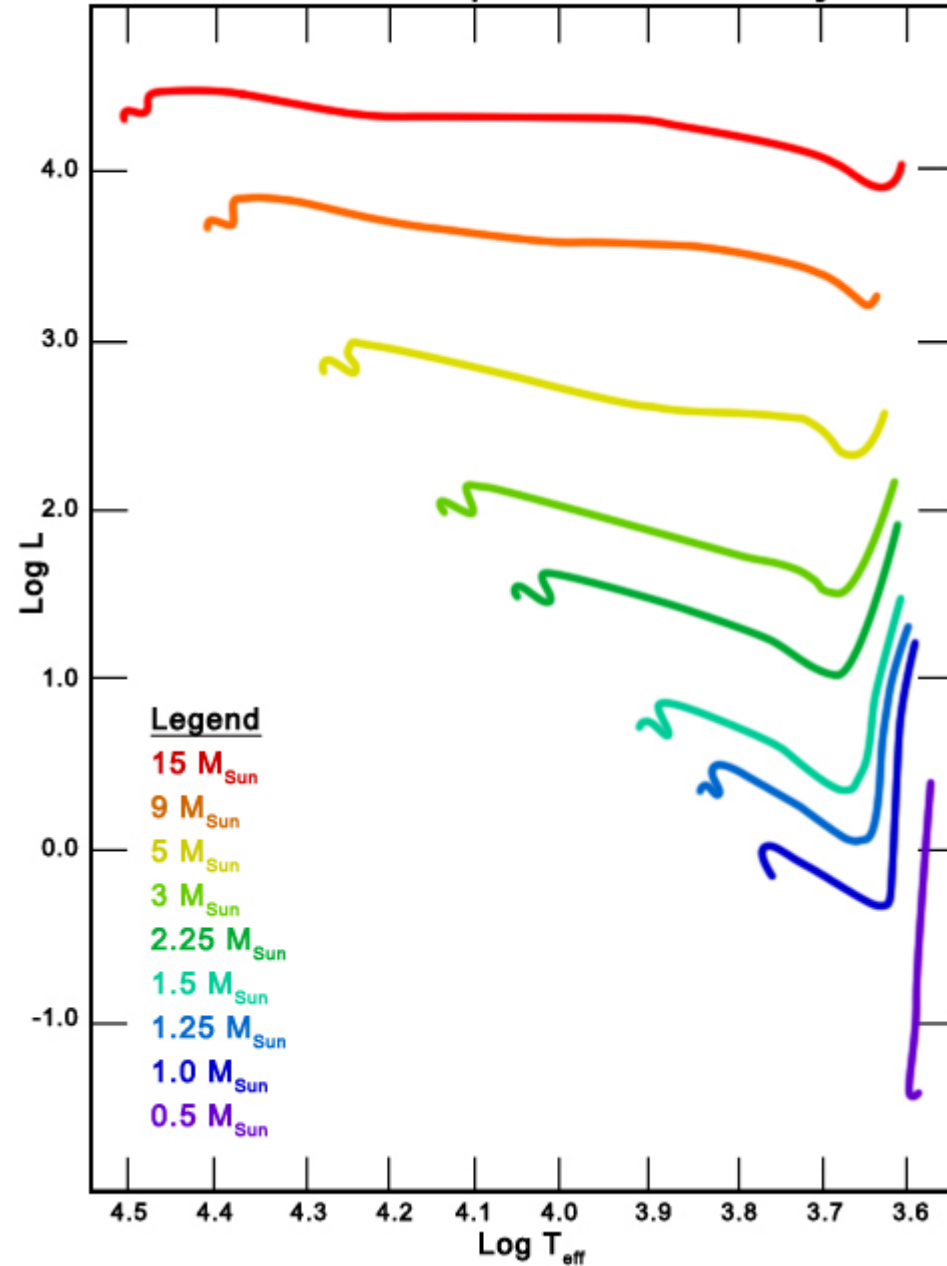
(Lada 1987 + André, Ward-Thompson, Barsony 1993)

## Early evolution

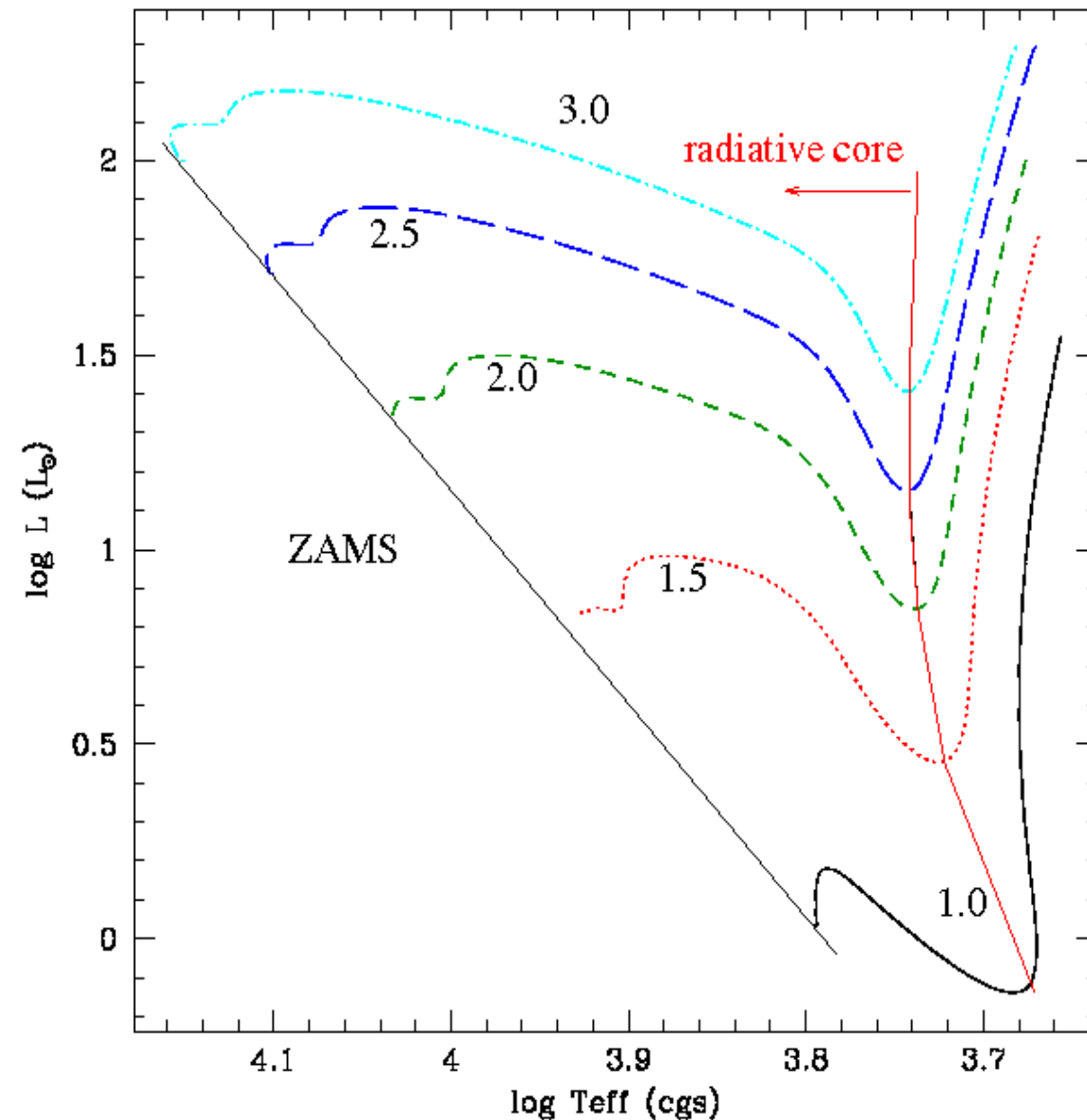


# Pre-main sequence evolution

Theoretical Pre-Main Sequence Evolutionary Tracks



# Pre-main sequence evolution



Stars contract and for the low-mass ones, they do it along the *Hayashi track* → Kelvin-Helmoltz timescale

D burning

P and density increase in core → increased T in core → increased ionisation → decreased opacity → radiative core appears

Li burning

→ now move to Henyey track

→ increased core temperature : partial CNO burning → small convective core in solar-type stars until  $^{12}\text{C}$  exhaustion

→ ppl chains take over

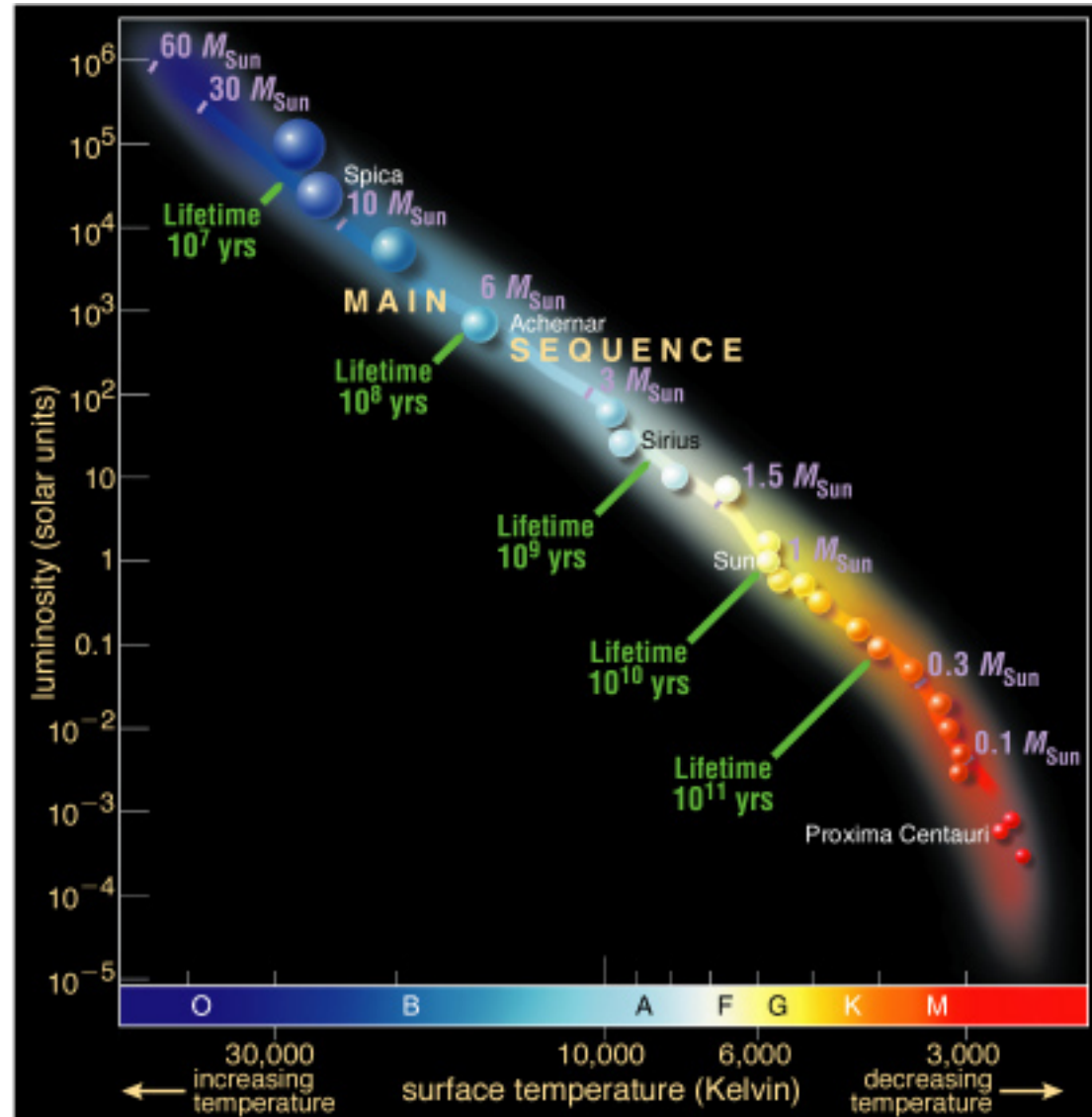
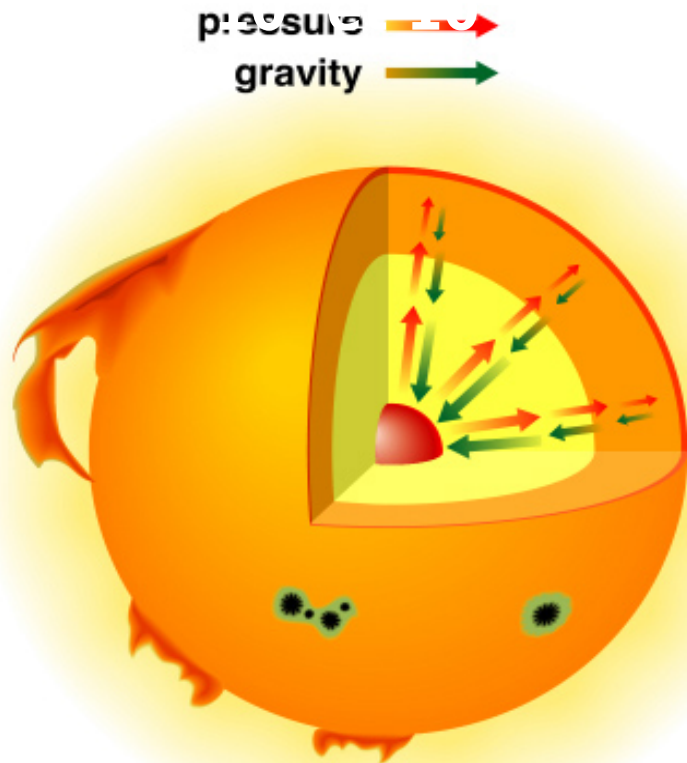
Zero Age Main Sequence (ZAMS)

# Main sequence evolution

Core H fusion

hydrostatic equilibrium

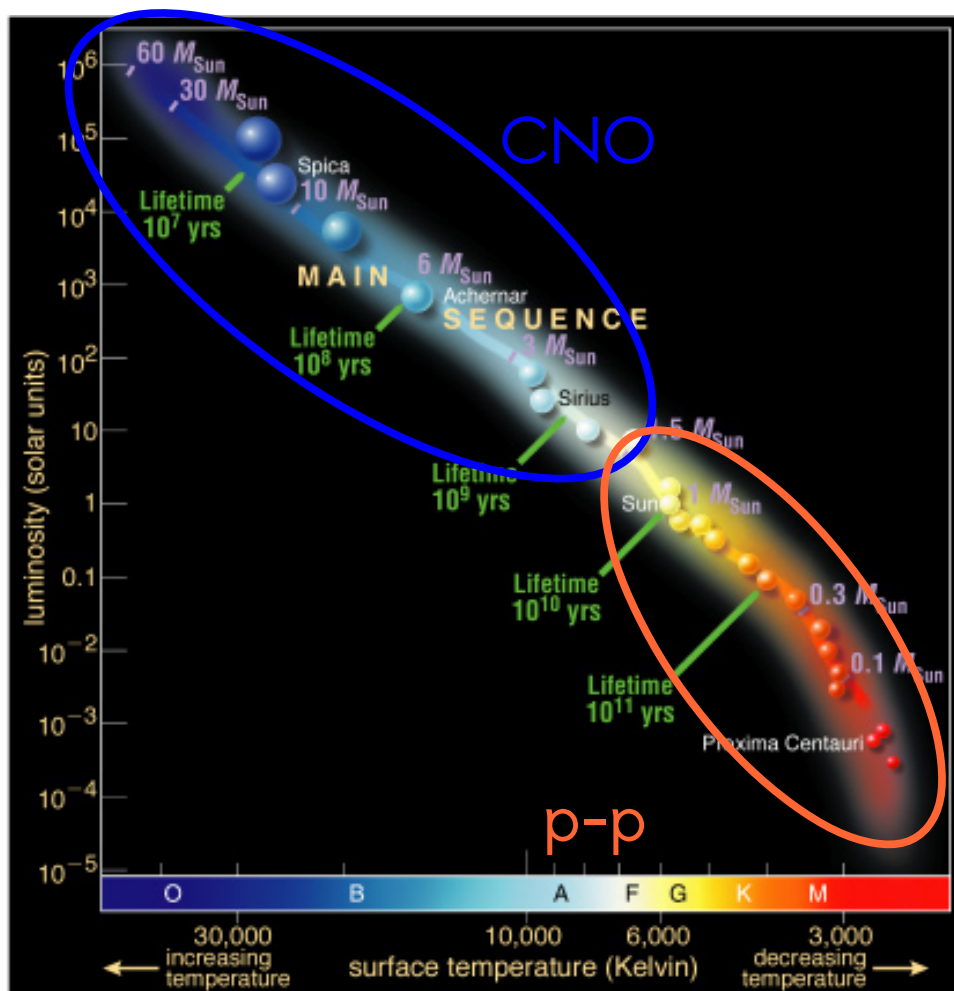
Duration of main sequence  
depends on  $T_c$  and  $\rho_c$



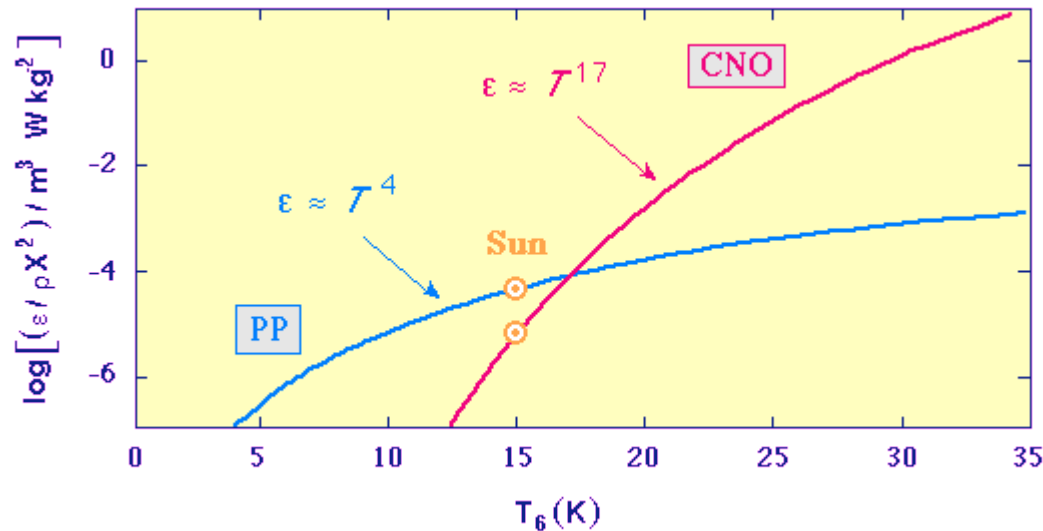


# Hydrogen burning

Core hydrogen burning occurs in main sequence stars via different reaction chains depending on the core temperature



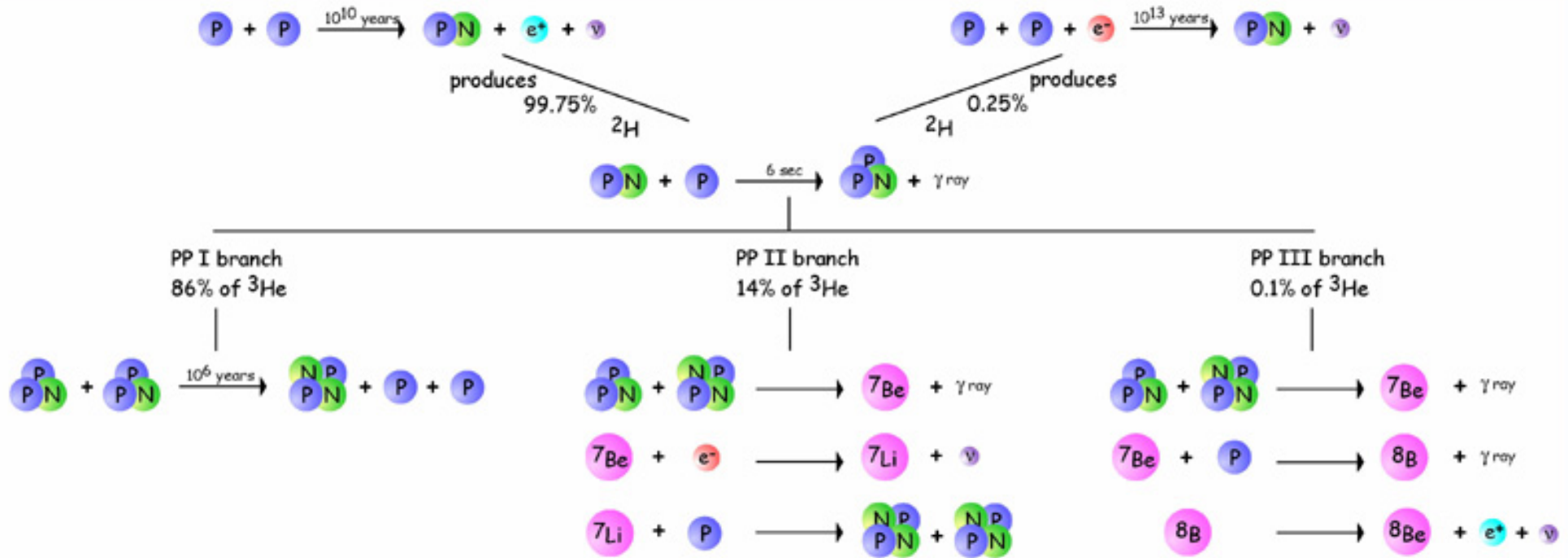
For a typical ratio  $X_{\text{CN}}/X_{\text{H}} = 0.02$



© Mike Guidry

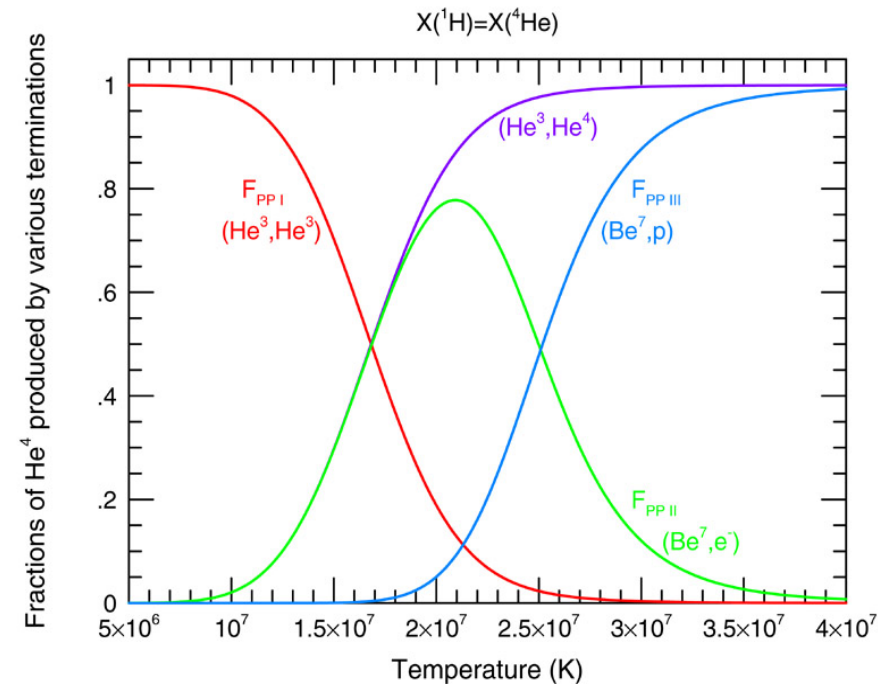
copyright Addison Wesley

# Hydrogen burning

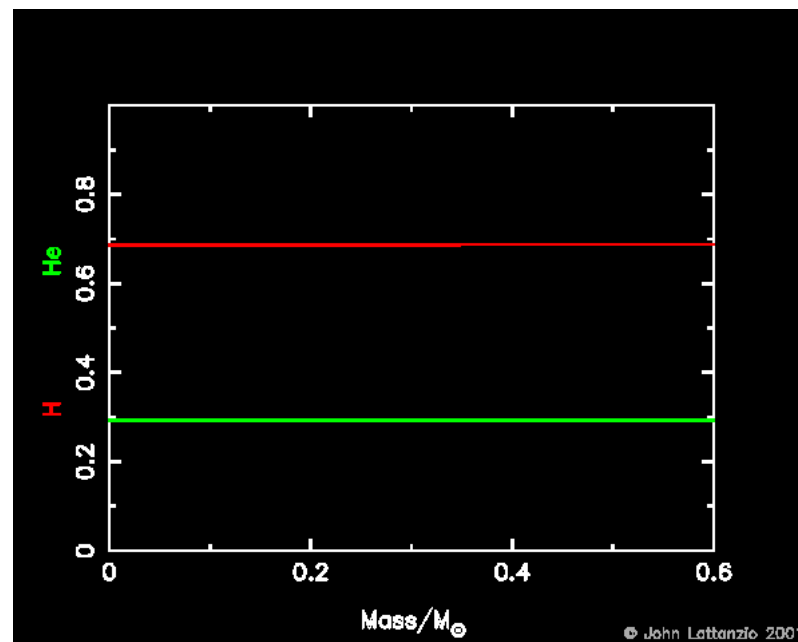
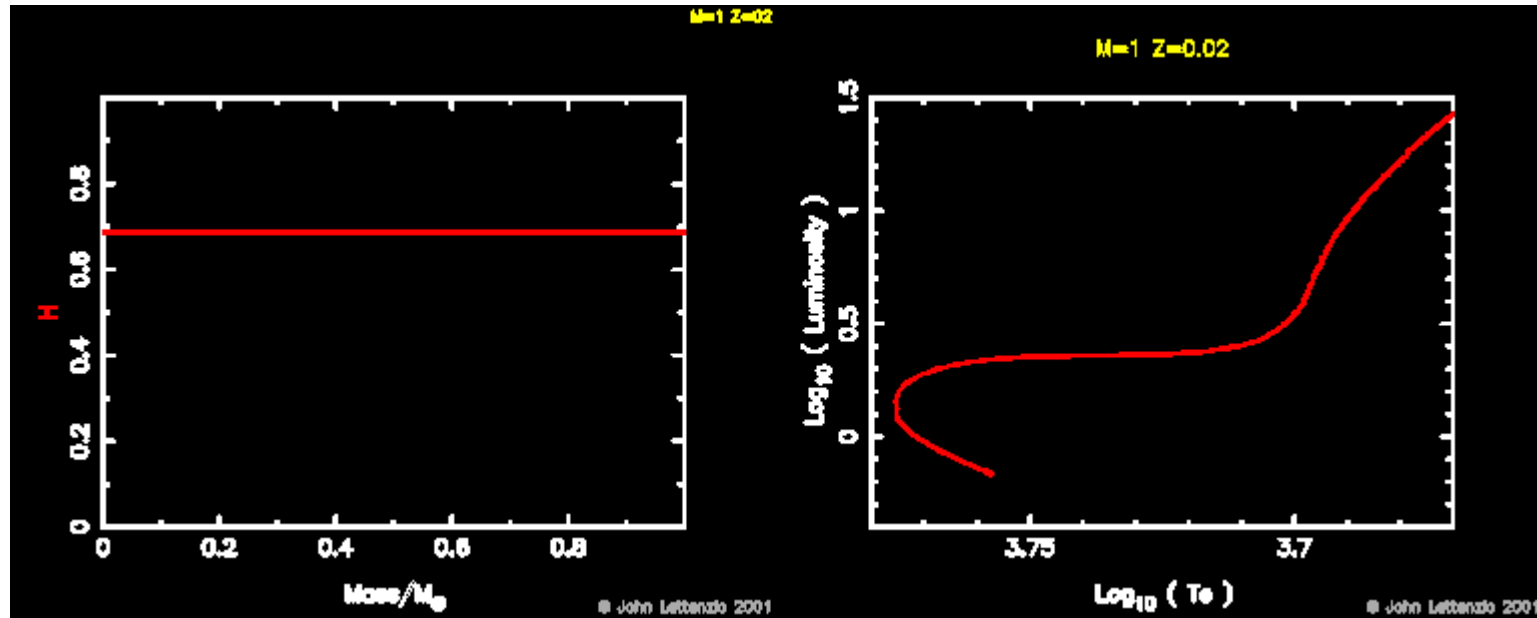


The weights of the reactions are given for conditions in the Sun. The PP chains are the most important energy source in stars.

Low mass stars ( $T_c \leq 1.7 \times 10^8 \text{ K}$ )

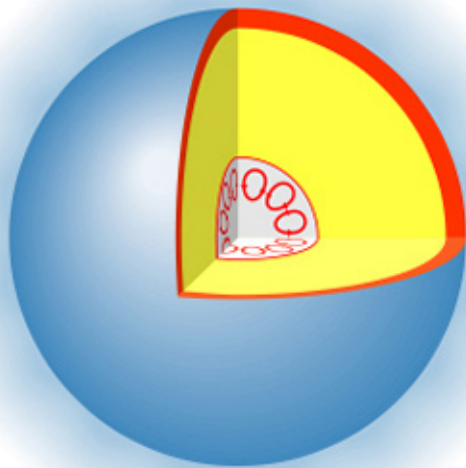


# Main sequence evolution of a 1Msun star



# Main Sequence

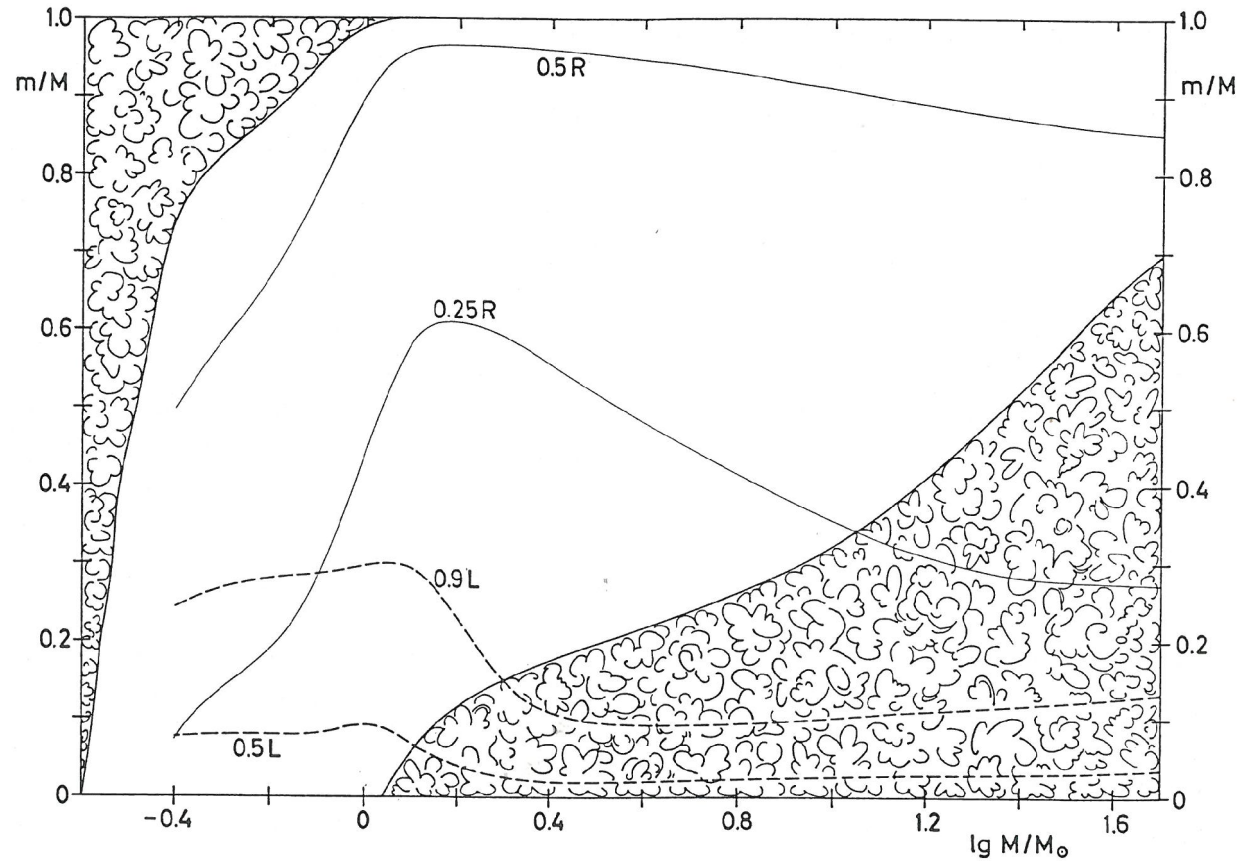
high-mass star



$1M_{\text{Sun}}$  star



very low mass star



**Fig.22.7.** The mass values  $m$  from centre to surface are plotted against the stellar mass  $M$  for the same zero-age main-sequence models as in Fig. 22.1. “Cloudy” areas indicate the extension of convective zones inside the models. Two solid lines give the  $m$  values at which  $r$  is  $1/4$  and  $1/2$  of the total radius  $R$ . The dashed lines show the mass elements inside which 50% and 90% of the total luminosity  $L$  are produced

# Main Sequence

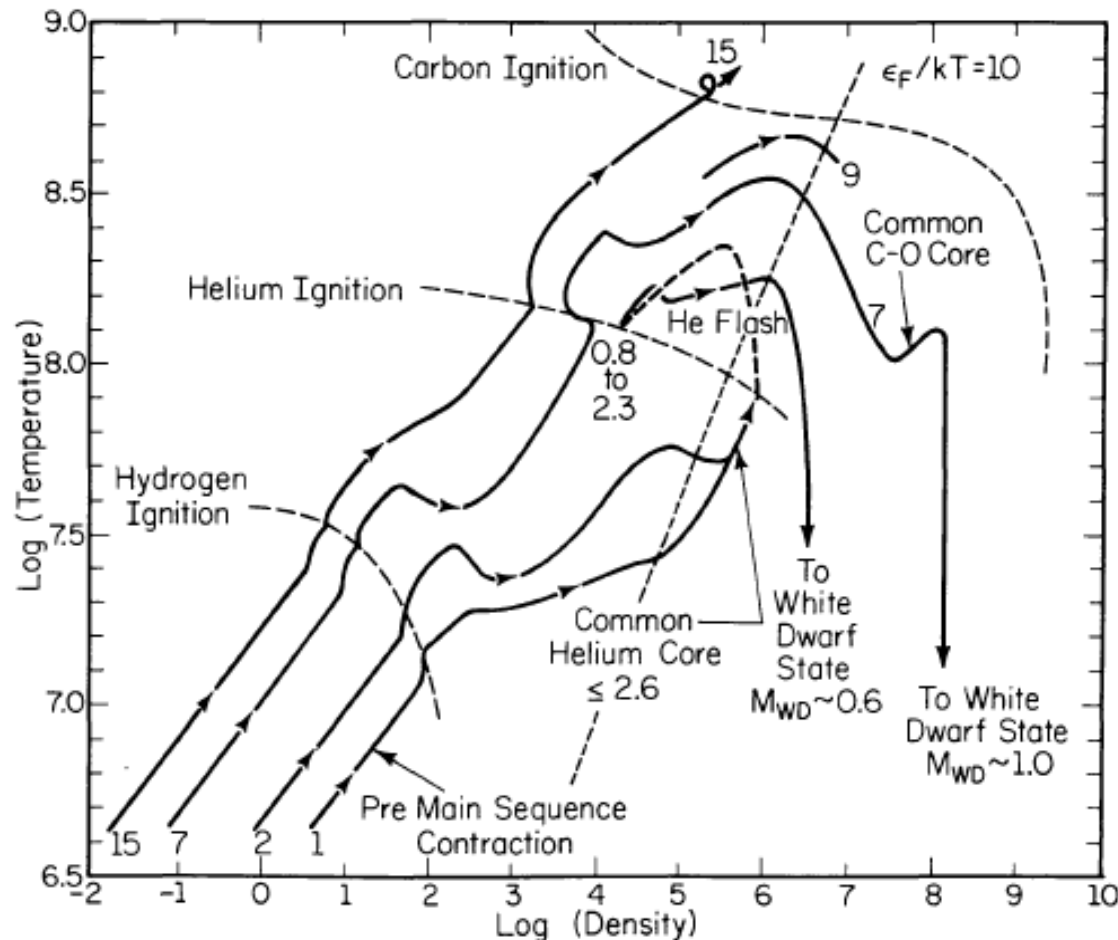
Main sequence stars are supposed to reflect the chemical composition of the ISM they were born out of.

Light elements (Li, Be, B) can be partially destroyed during the PMS and appear depleted on the main sequence

No abundance variation of heavy elements is expected at the stellar surface during this phase compared with the initial content



# Post Main Sequence evolution

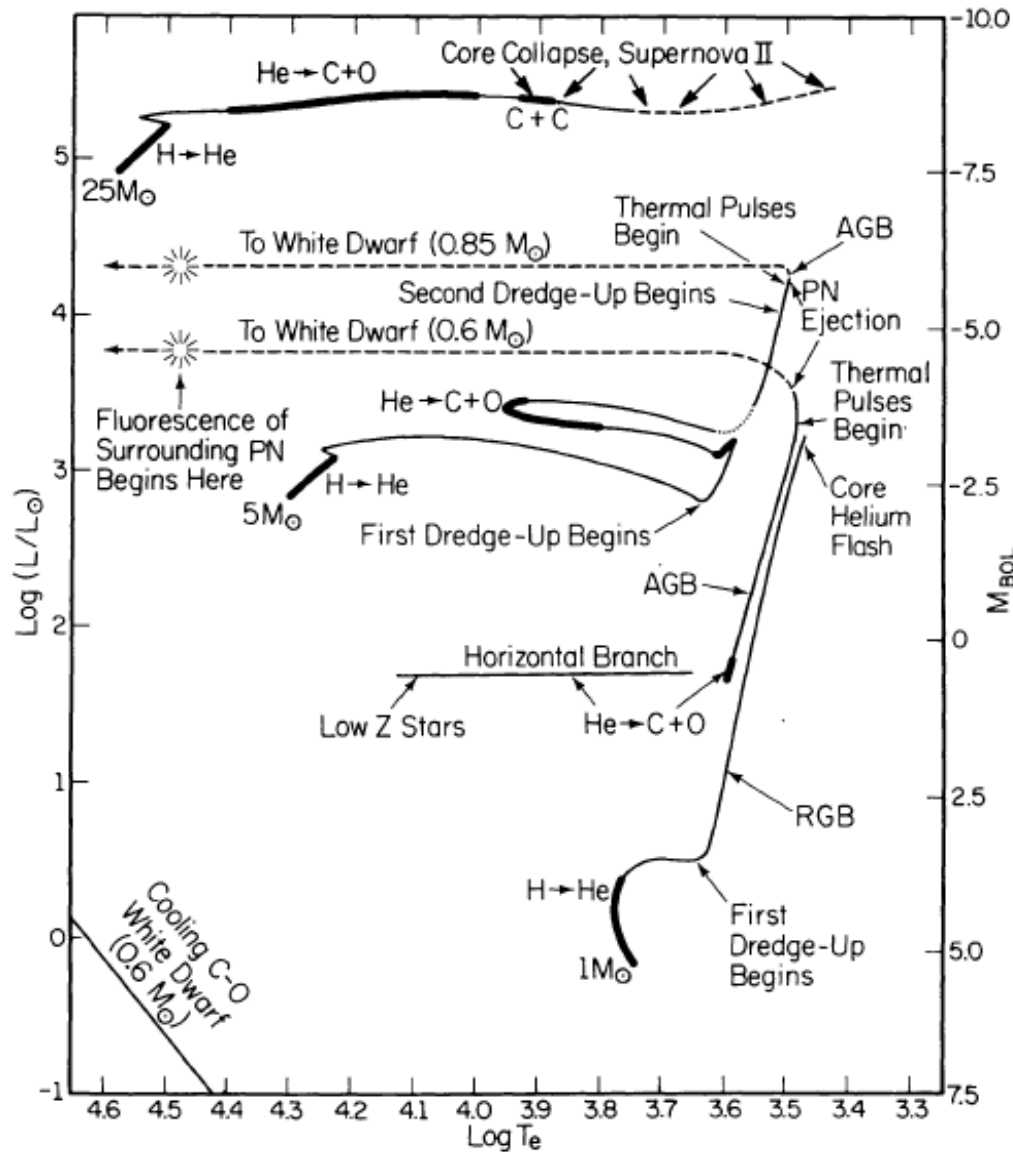


Evolution (beyond the MS) is mainly dictated by the evolution of  $T$  and density in the core, which determine the nuclear energy production.

The path in the HR diagram will also be influenced by modifications of the opacity in the external layers.

Stars of different masses will have different evolutions.

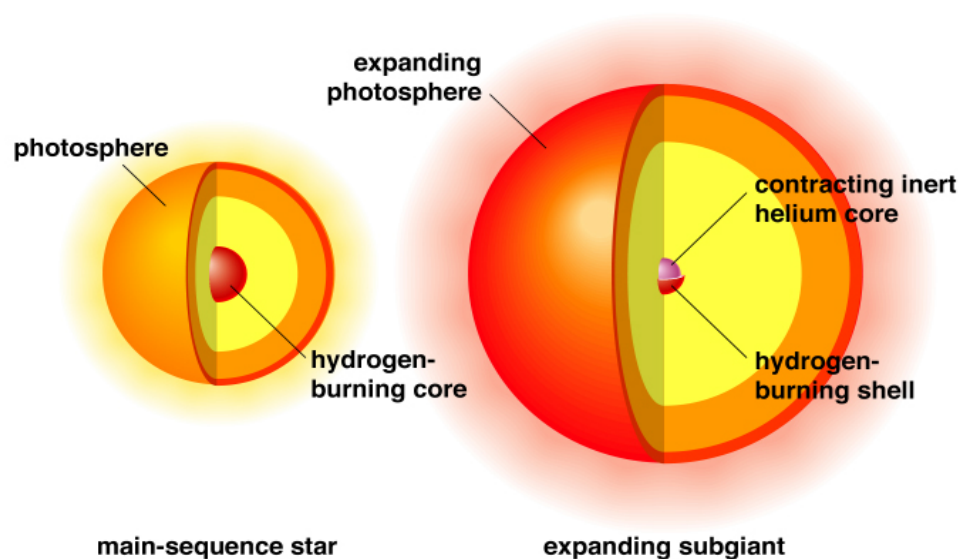
# Post Main Sequence evolution



Succession of phases of hydrostatic equilibrium and non-equilibrium phases (contraction/expansion) during which the star temperature decreases (for low and intermediate mass stars).

# Post-Main sequence evolution of low-mass stars

Increase of potential gravitational energy in the stellar centre at central H exhaustion → core contraction

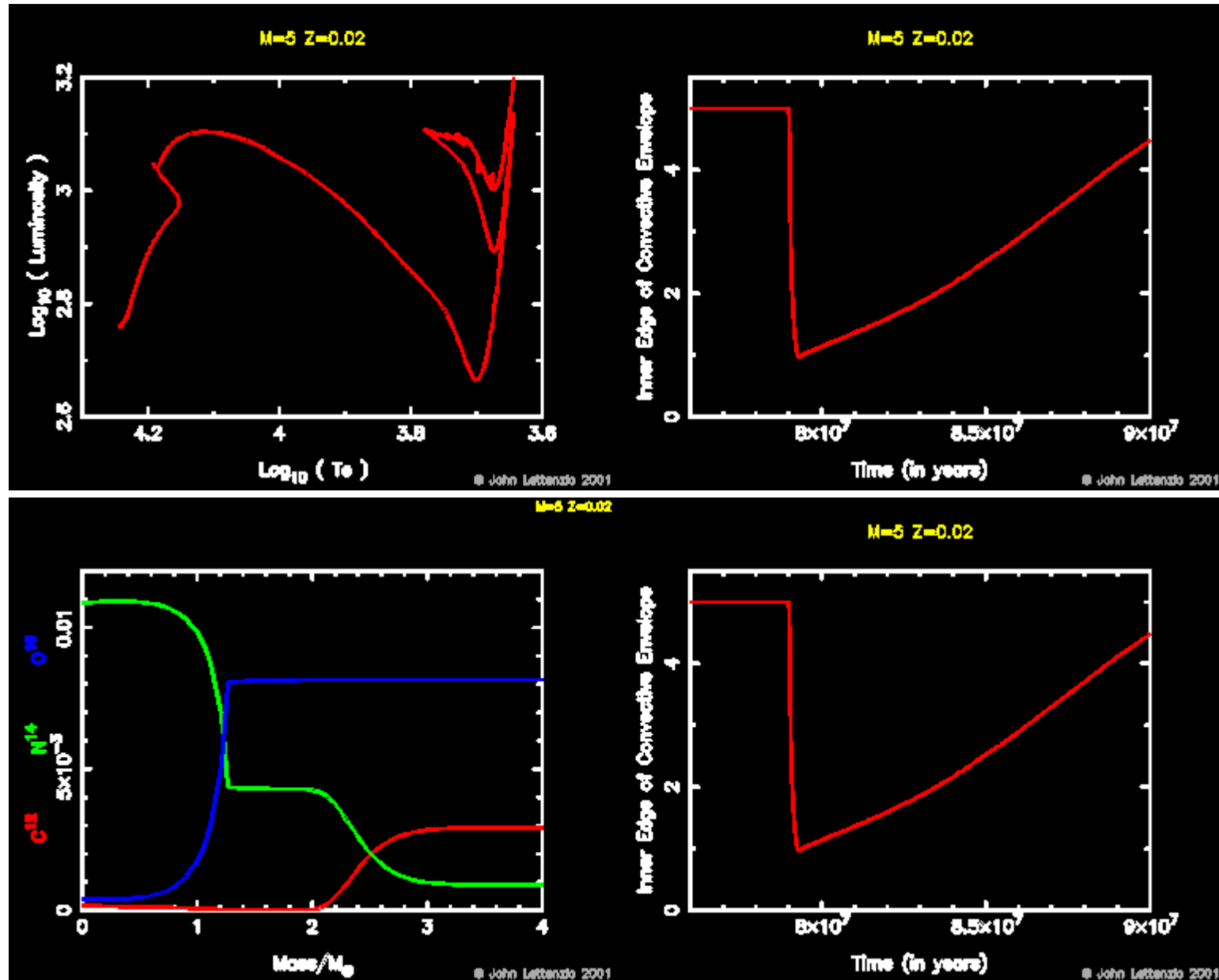


Copyright © Addison Wesley

Temperature continuity →  $T$  increases in regions surrounding the core → HBS  
 $T$  increases in central regions → expansion of envelope to maintain the temperature gradient → the star moves to the right in the HR diagram

Cooling associated with radius increase  
→ increased opacity in external layers  
→ deepening of the convective envelope → **first dredge-up**

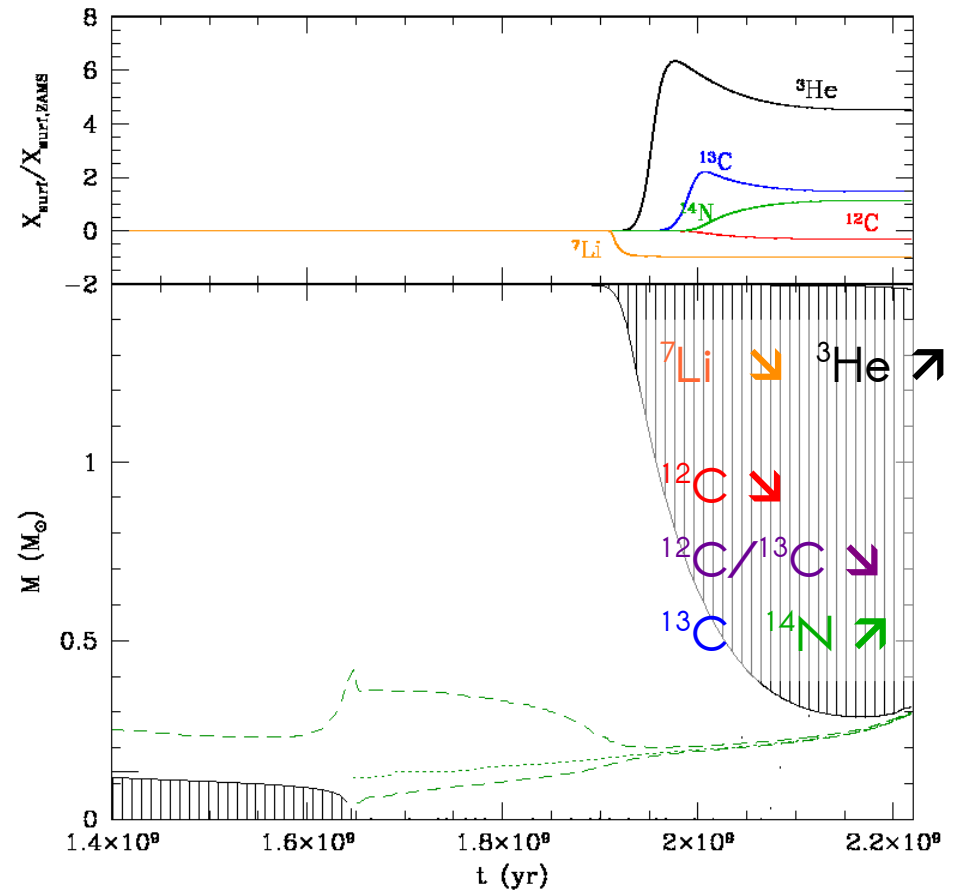
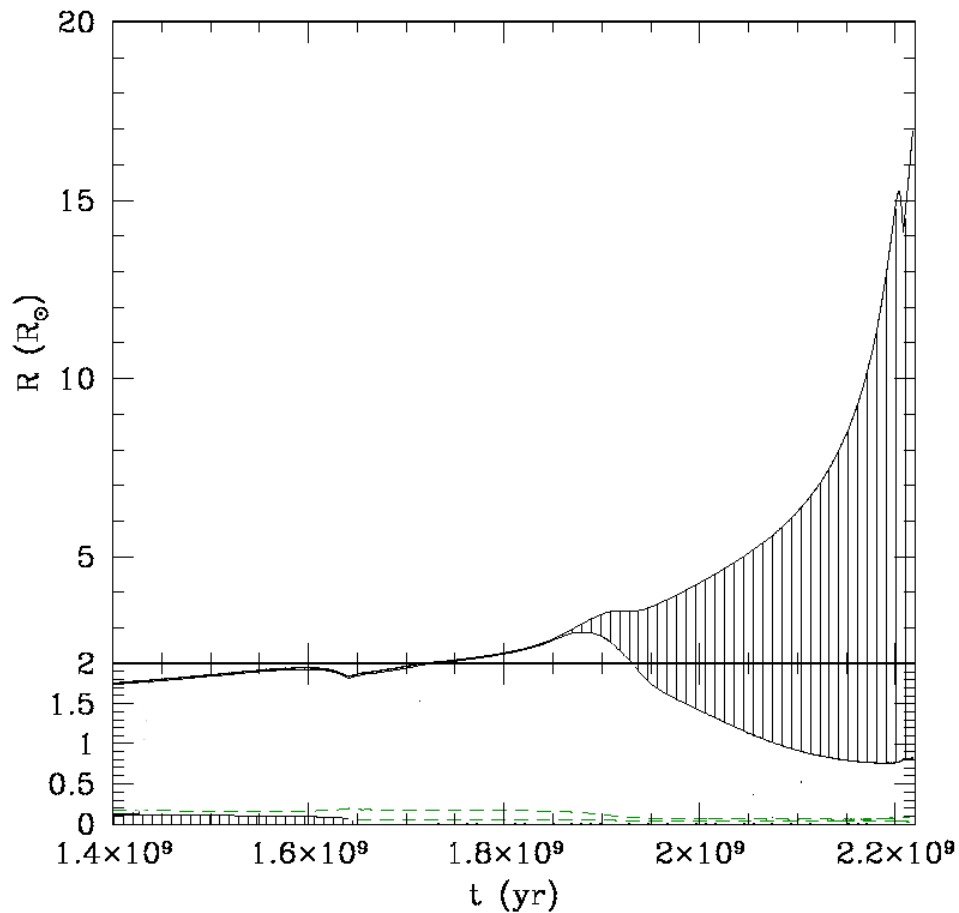
# First dredge-up



# First dredge-up

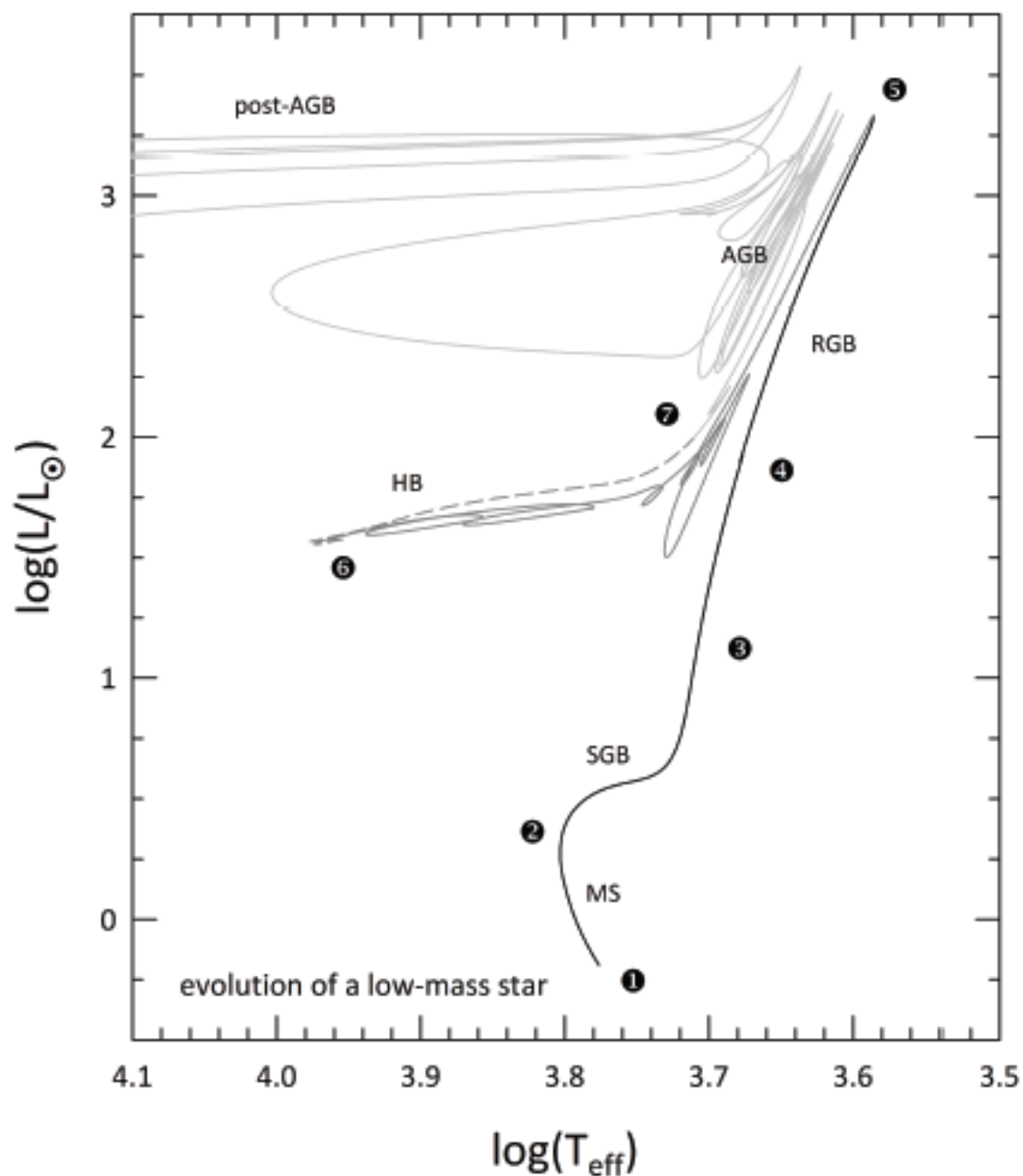
Deepening of the convective envelope in mass reaching regions that have been processed through nuclear reactions →

Stellar surface abundances modification





# Post-Main sequence evolution of low-mass stars



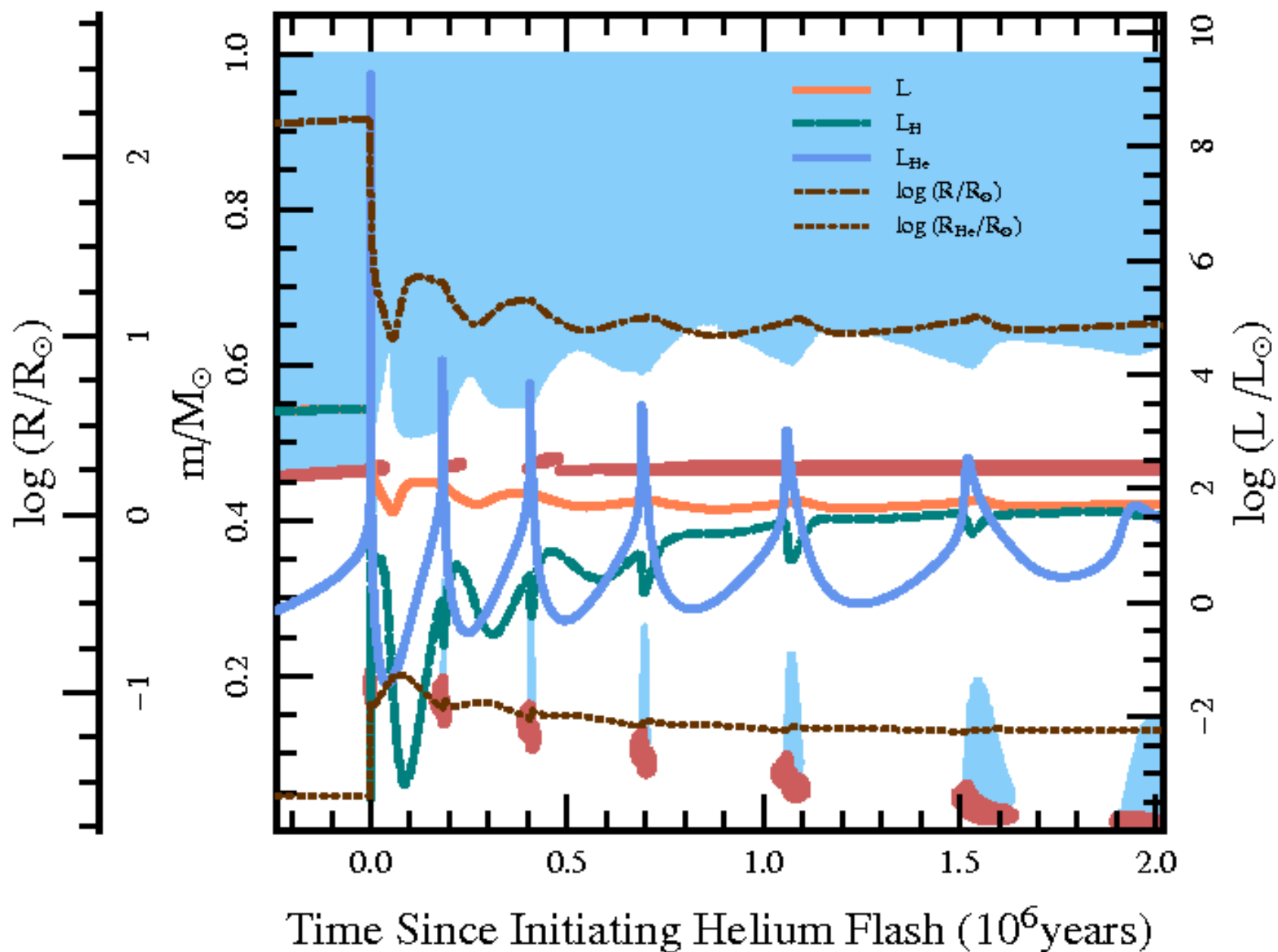
RGB stars have a partially degenerated core  $\rightarrow$  evolves independently of temperature variations.

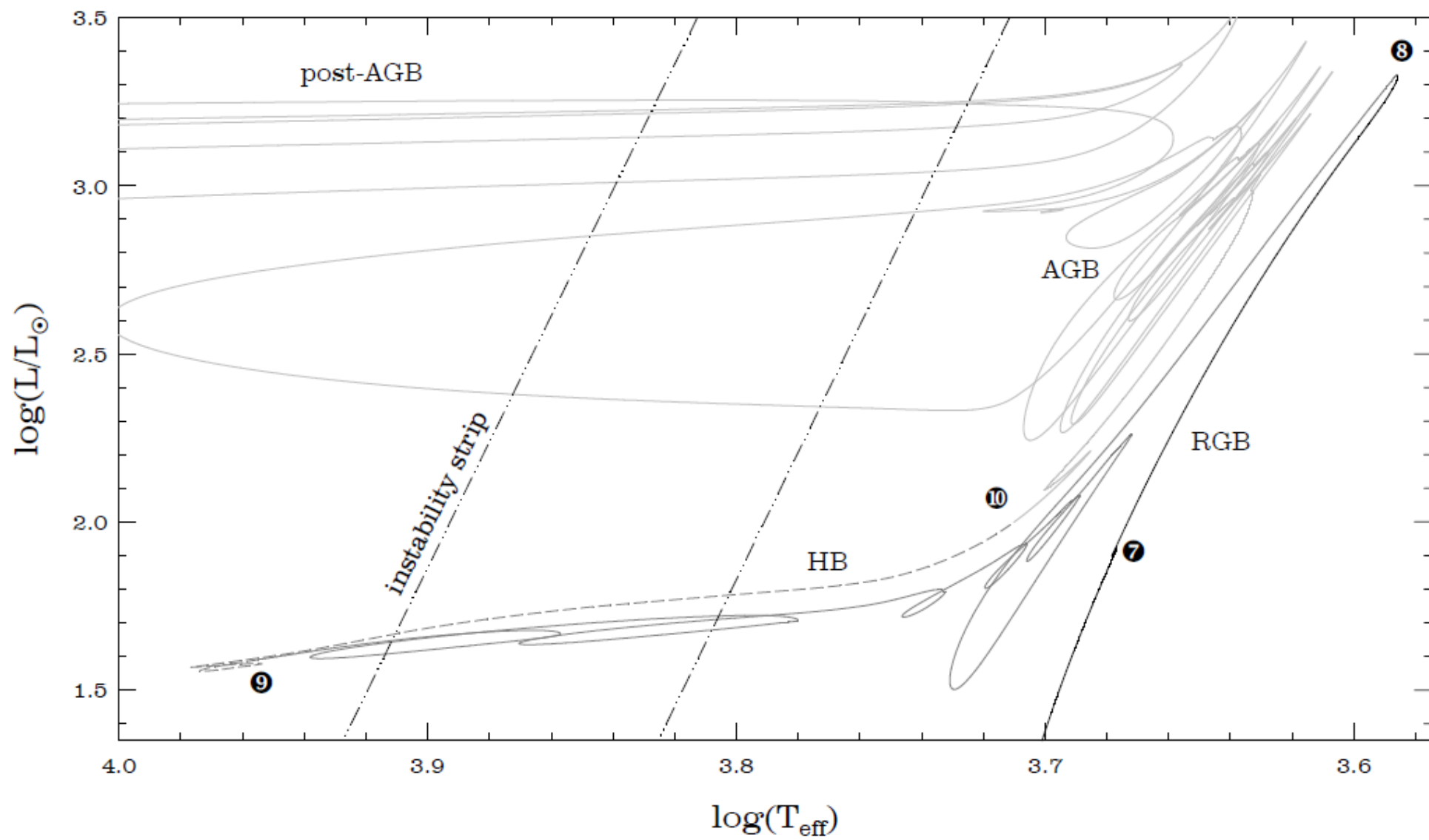
Core mass increases in core regions as the stars ascend the RGB

When the core mass reaches  $0.45 M_{\odot}$ , and  $T_c$  and  $\rho_c$  get large enough  $\rightarrow$  He fusion reactions ignite in degenerate medium

**Helium flash**

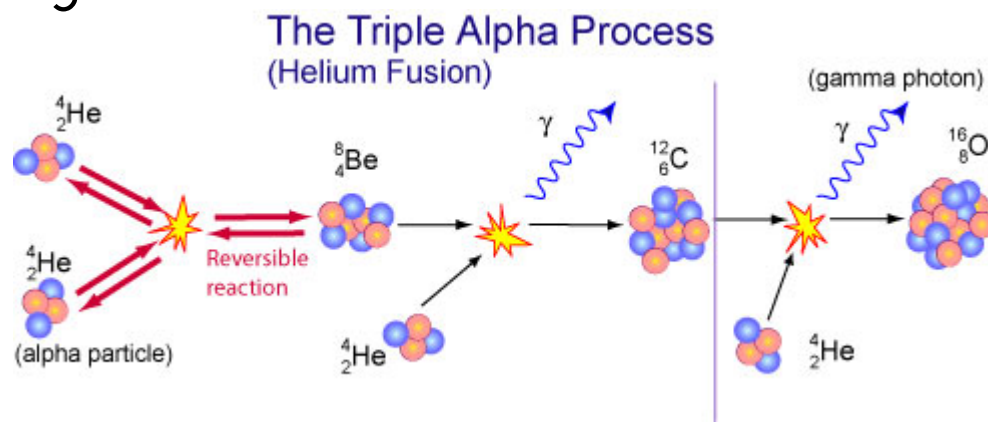
# He flash





# He burning / red clump

$3\alpha$  reactions dominate the energy production in He rich regions with  $T_c > 10^8$  K and  $\rho_c > 10^5$  g/cm<sup>3</sup>



© Copyright CSIRO Australia 2004.

These reactions will start in partially degenerated plasma in low-mass stars

## Helium Flash

### He fusion products

Carbon  ${}^{12}\text{C}$

${}^4\text{He}(\alpha, \gamma){}^8\text{Be}(\alpha, \gamma){}^{12}\text{C}$

Oxygen  ${}^{16}\text{O}$ ,  ${}^{18}\text{O}$

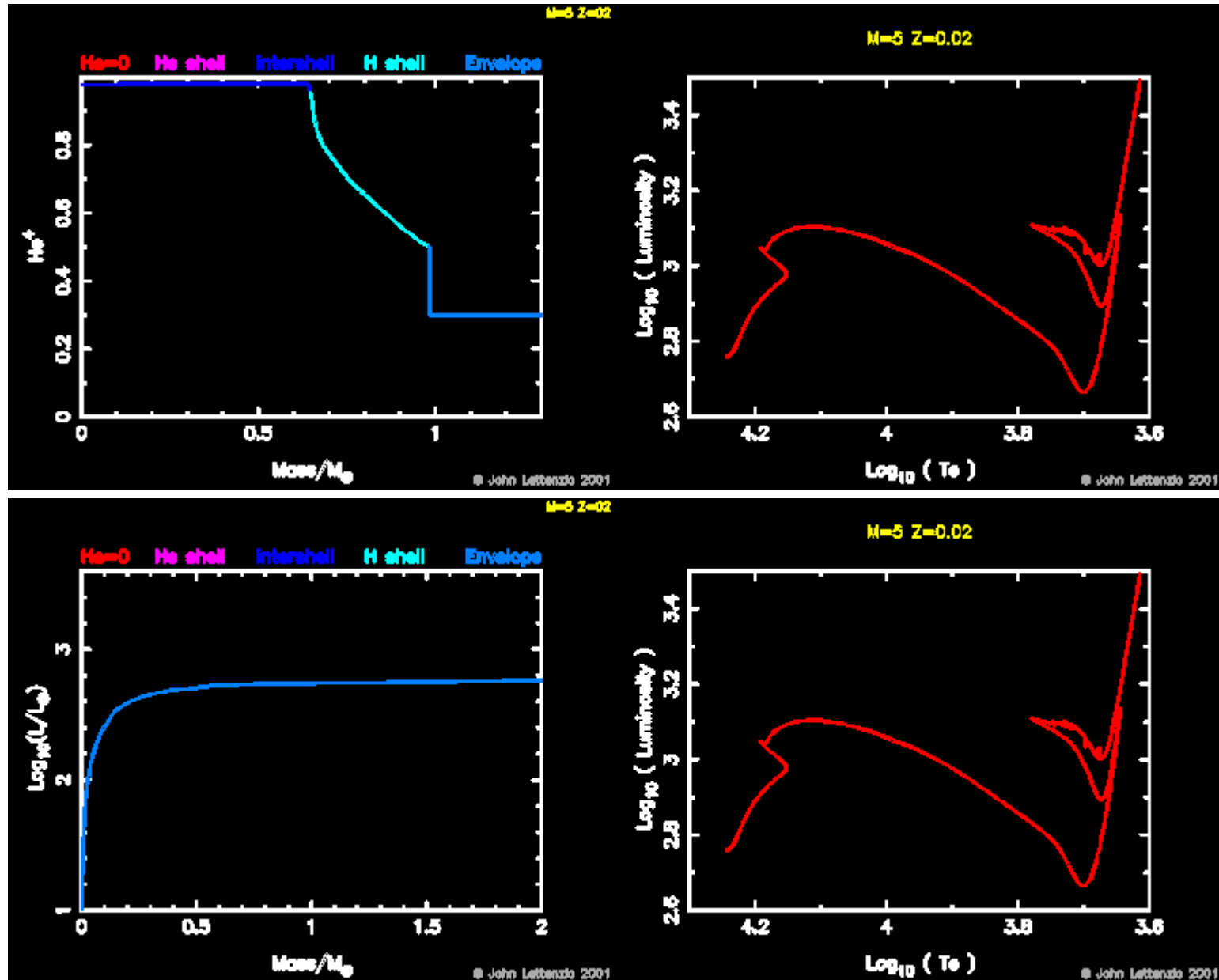
${}^{12}\text{C}(\alpha, \gamma){}^{16}\text{O}(\alpha, \gamma){}^{20}\text{Ne}$

Neon  ${}^{20}\text{Ne}$ ,  ${}^{22}\text{Ne}$

neutrons via

${}^{13}\text{C}(\alpha, n){}^{16}\text{O}$  et  ${}^{22}\text{Ne}(\alpha, n){}^{25}\text{Mg}$

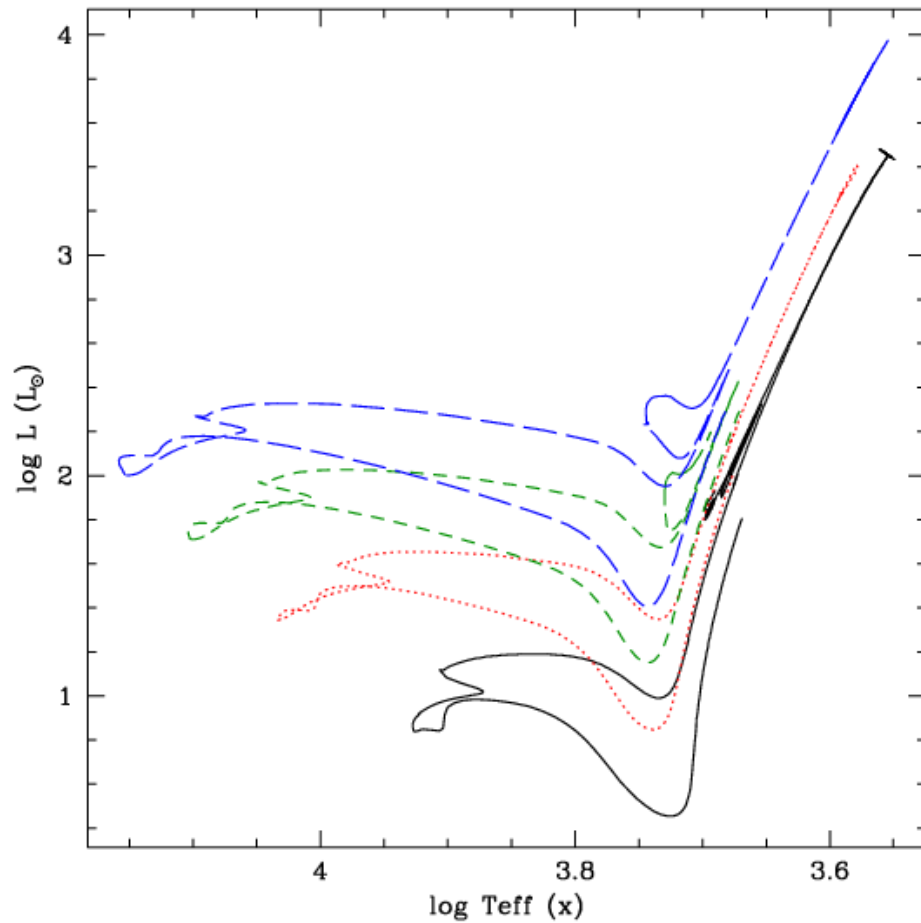
# He burning / red clump - 5 Msun star



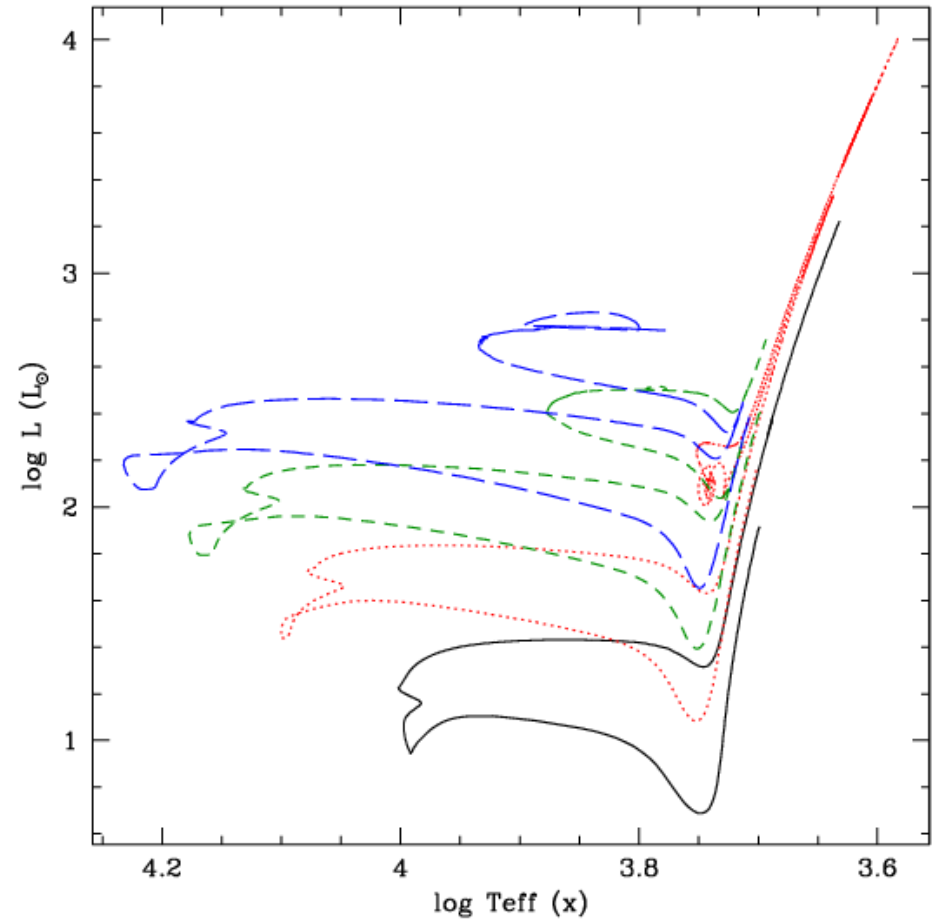


# Impact of metallicity on evolution

$[\text{Fe}/\text{H}] = -0.5$

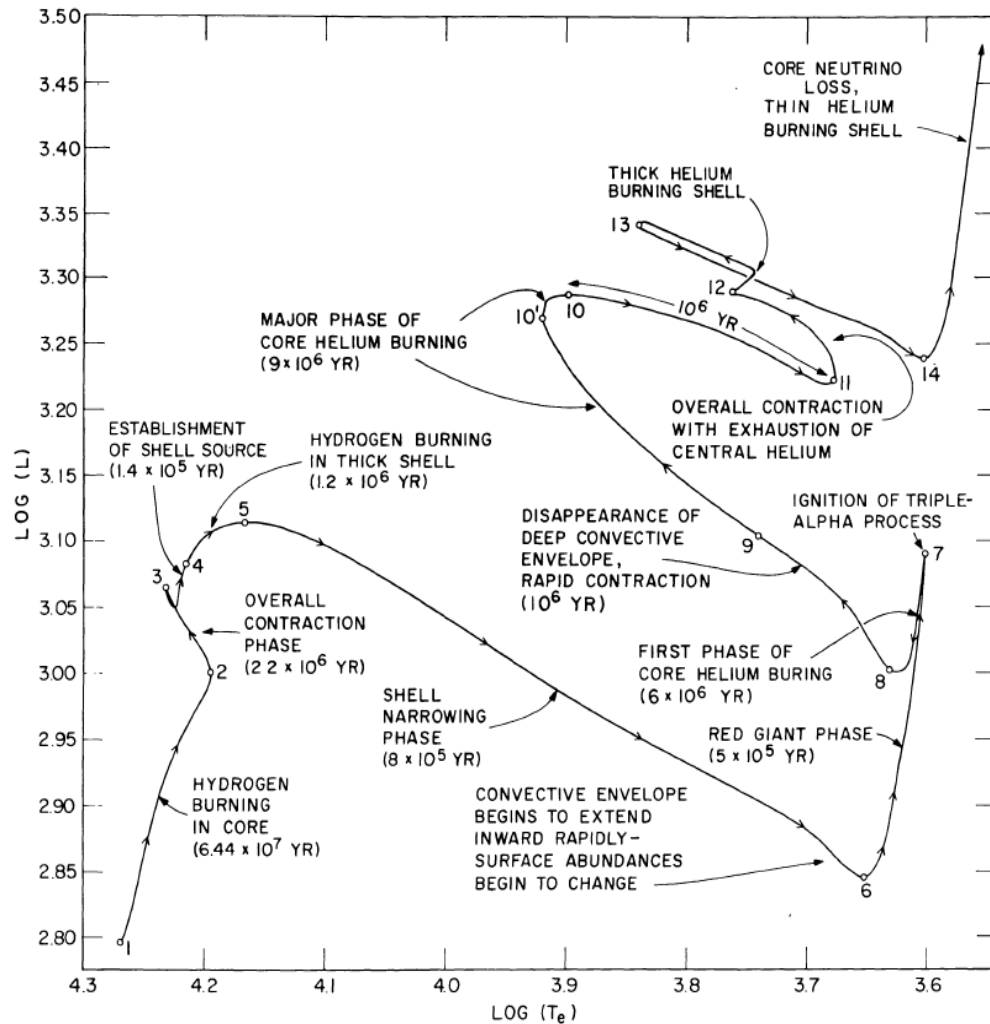


$[\text{Fe}/\text{H}] = -1.5$



Models between  $1.5 M_{\odot}$  and  $3 M_{\odot}$

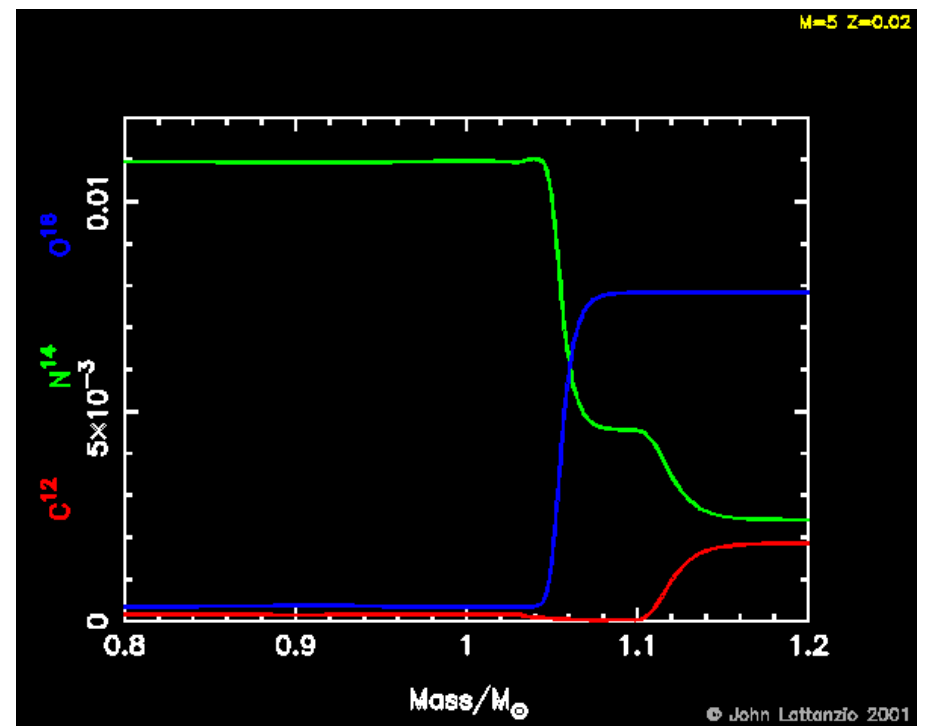
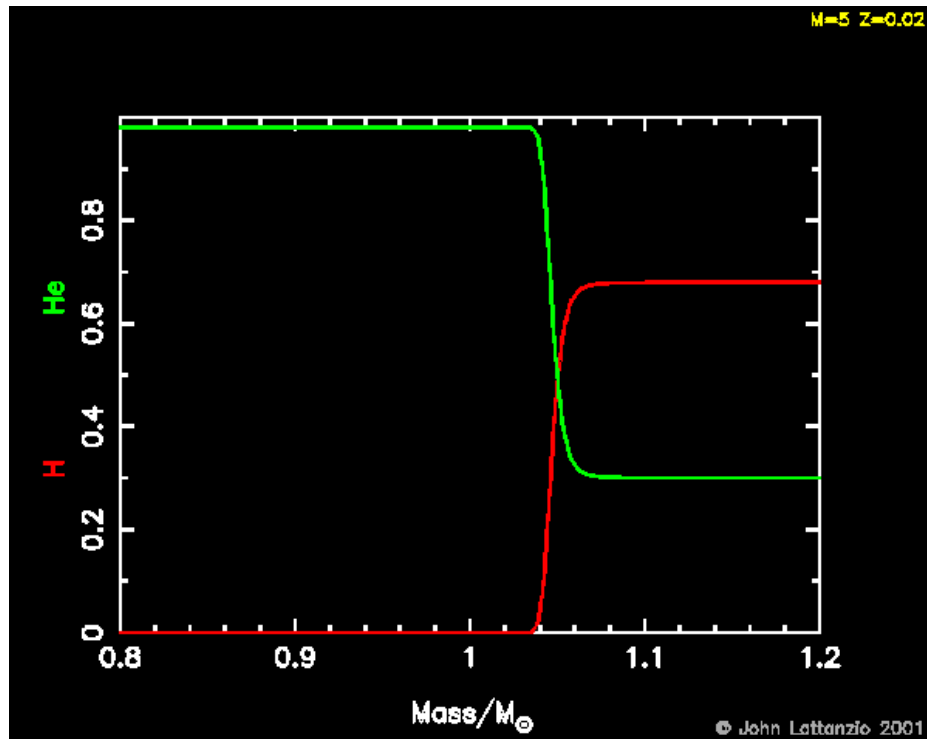
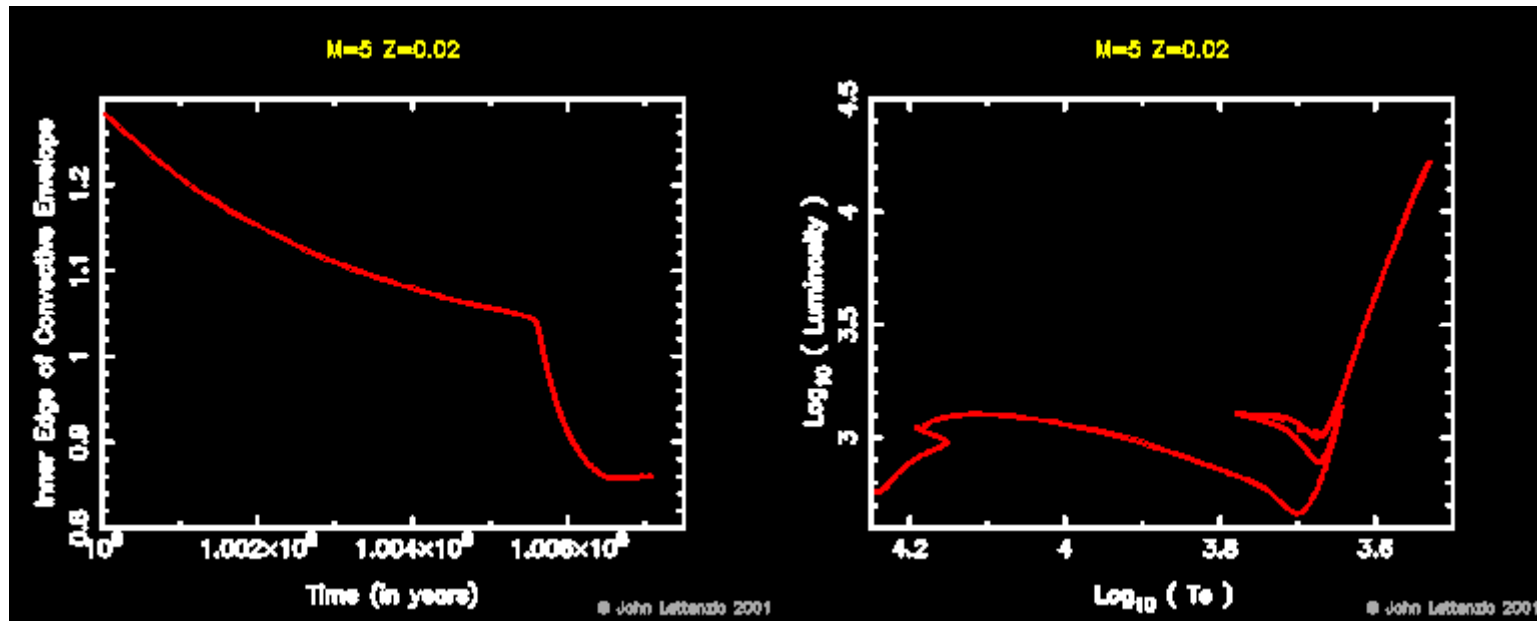
# Intermediate mass stars evolution and 2nd DUP



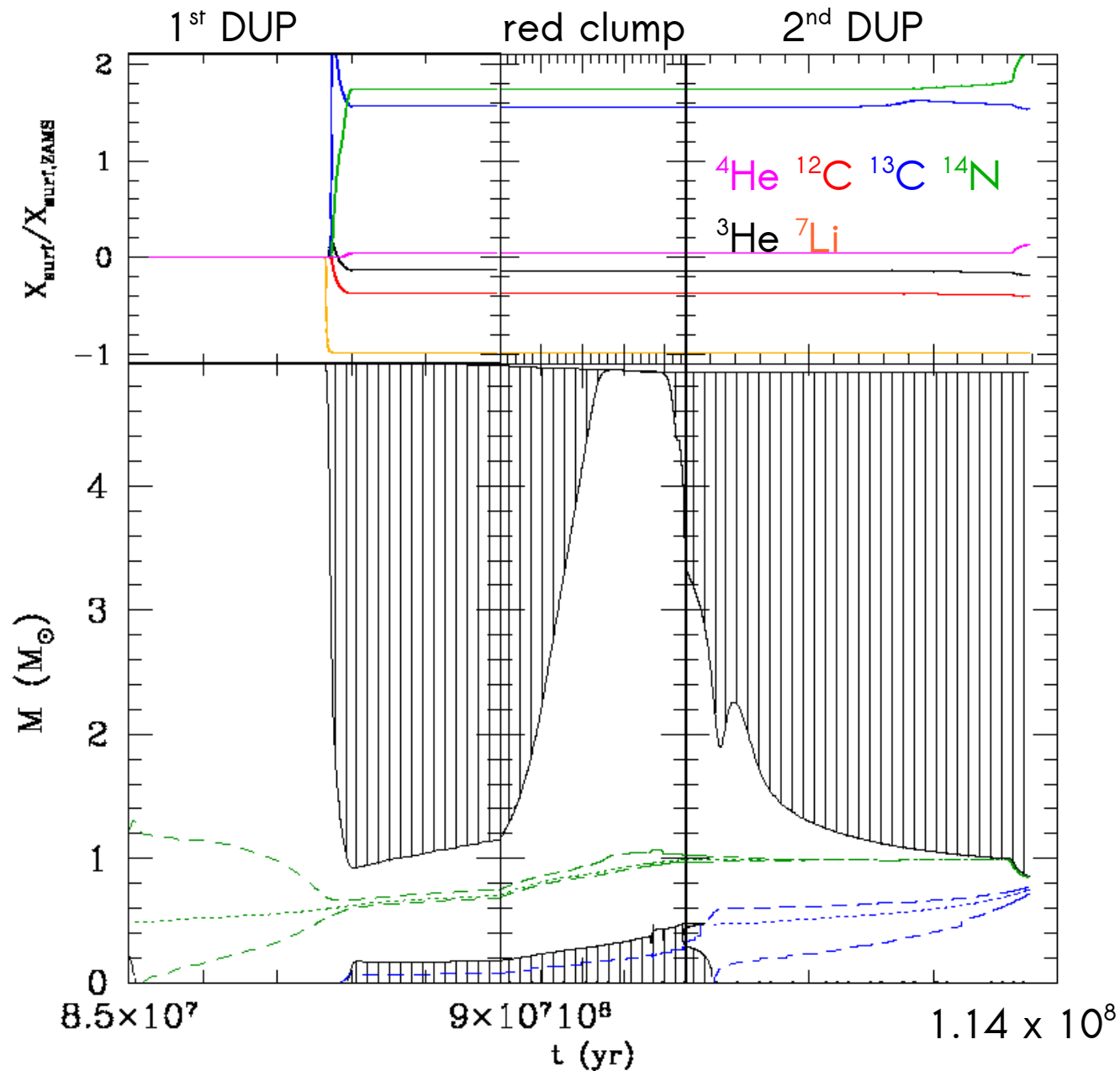
Core He fusion in non-degenerate plasma  $\rightarrow$  second dredge-up occurring at the end of the core He burning  $\rightarrow$  similar to 1st DUP.

FIG. 2.—The track in the H-R diagram of a theoretical model star of mass  $5 M_{\odot}$  and of Population I composition. Text beside various portions of the track describe an important physical process occurring within the star at the indicated position. From Iben (1967c).

# Intermediate mass stars evolution and 2nd DUP



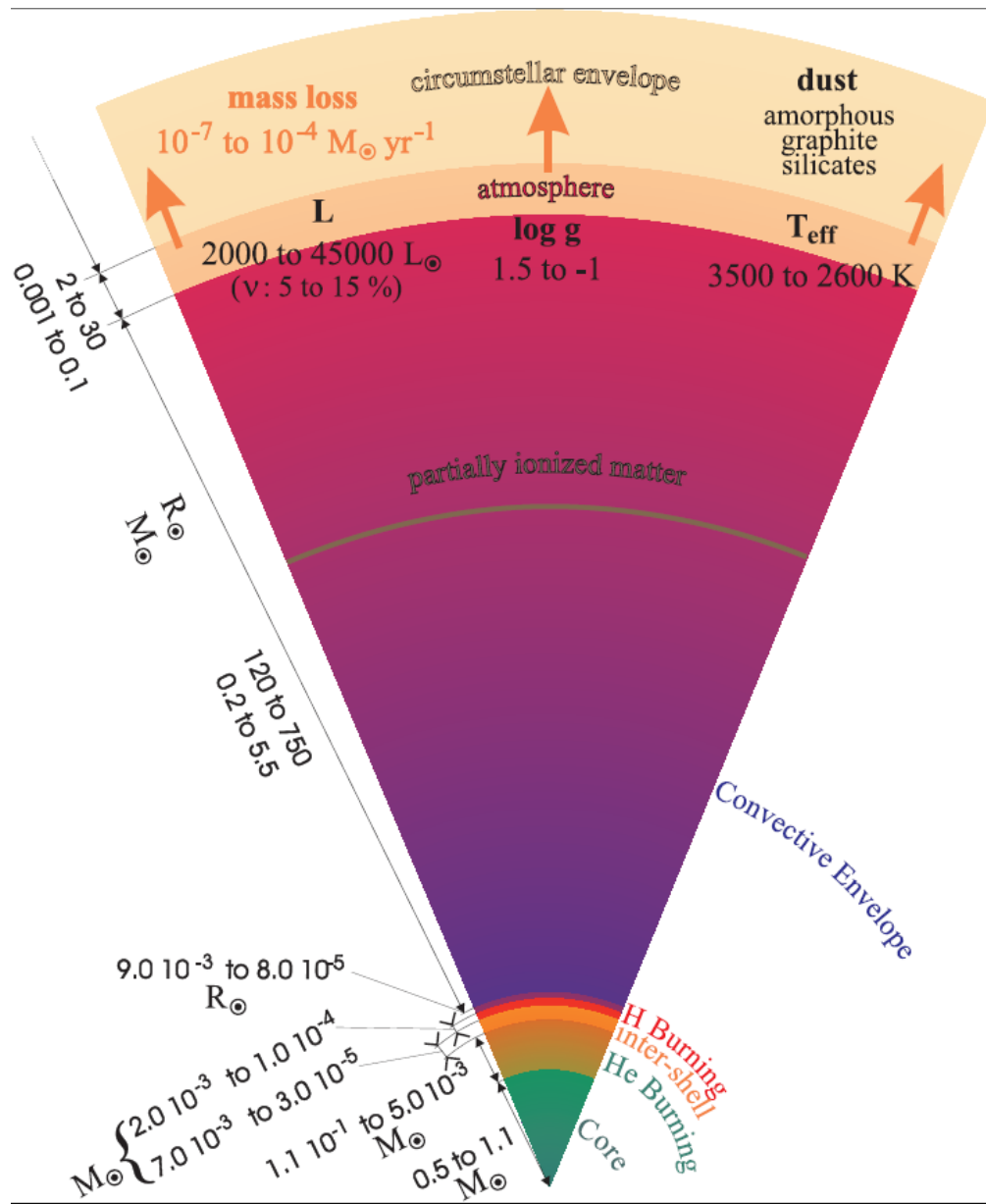
# Intermediate mass stars evolution and 2nd DUP



$5 M_{\odot}$  @ solar metallicity

After the 2nd DUP,  $^4\text{He}$  and  $^{14}\text{N}$  increase at the stellar surface

# AGB phase



Stars with masses  $\leq 10 M_{\text{sun}}$  ascend the red giant branch for the second time after core He burning  $\rightarrow$  AGB stars

Very luminous  $\rightarrow$  undergo important mass loss and peculiar nucleosynthesis due to double shell nuclear fusion

Essential contributors to the chemical evolution of interstellar medium

# TP-AGB phase

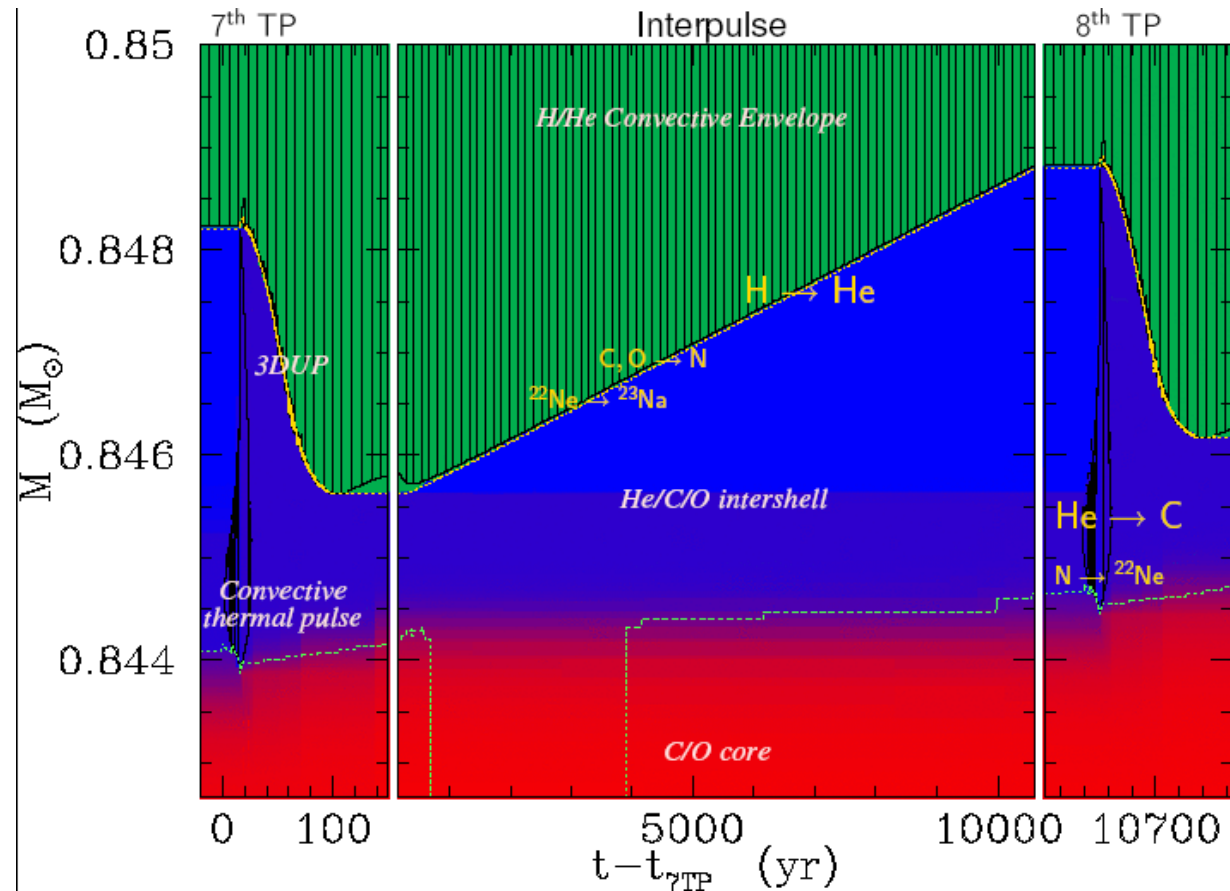
HBS et HeBS advance at different paces : intershell mass  $\nearrow$  ,  $T(\text{HeBS}) \nearrow$   
 $\rightarrow$  thermal pulse

The pulse swallows the products of H nuclear fusion  
**peculiar nucleosynthesis**

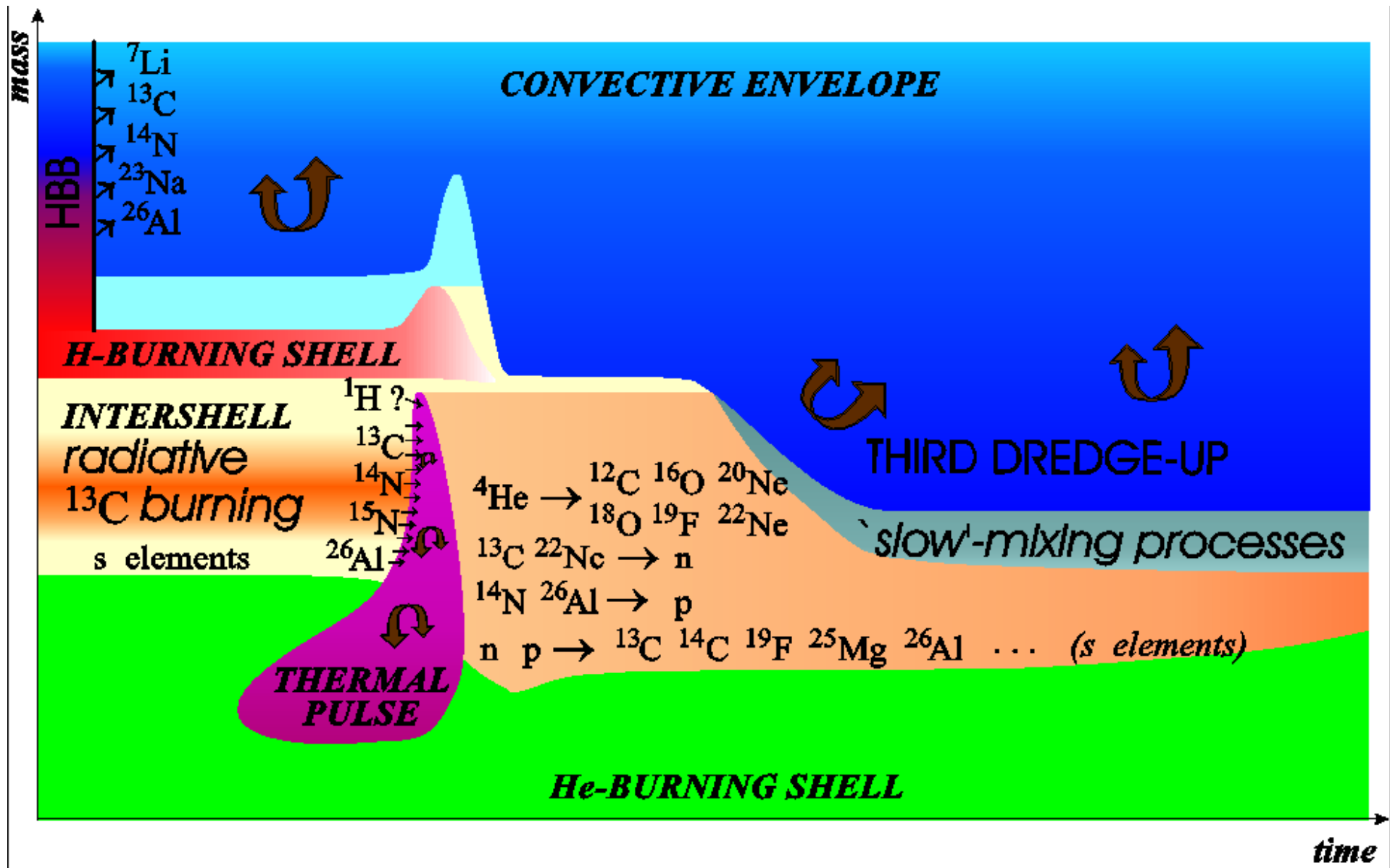
Pulse acts like a piston

- lifts up the envelope
- shuts down the HBS
- possibly further deepening of falling back envelope into regions processed in the pulse

3rd DUP events



# TP-AGB nucleosynthesis



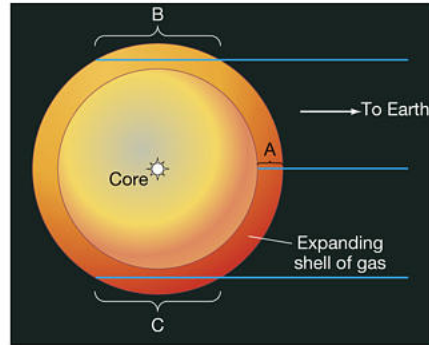
This is a way to increase C/O stellar atmospheres and to produce heavy neutron-rich elements



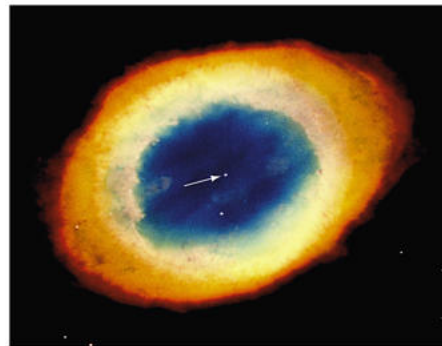
# Post-AGB evolution and PNae



(a)

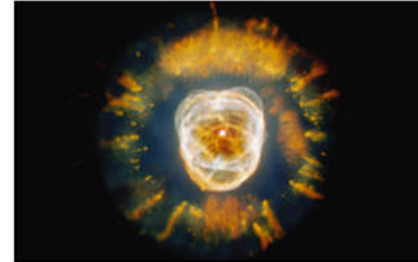


(b)



(c)

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(a)



(b)



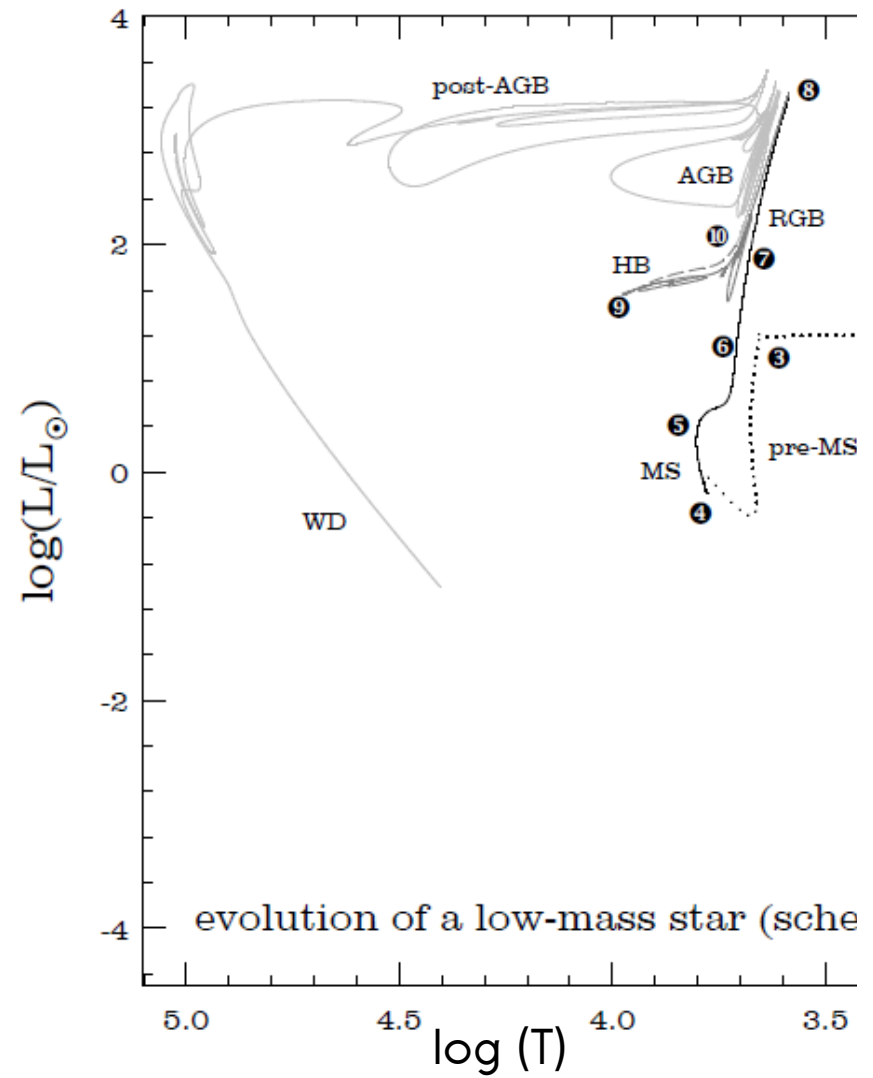
(c)

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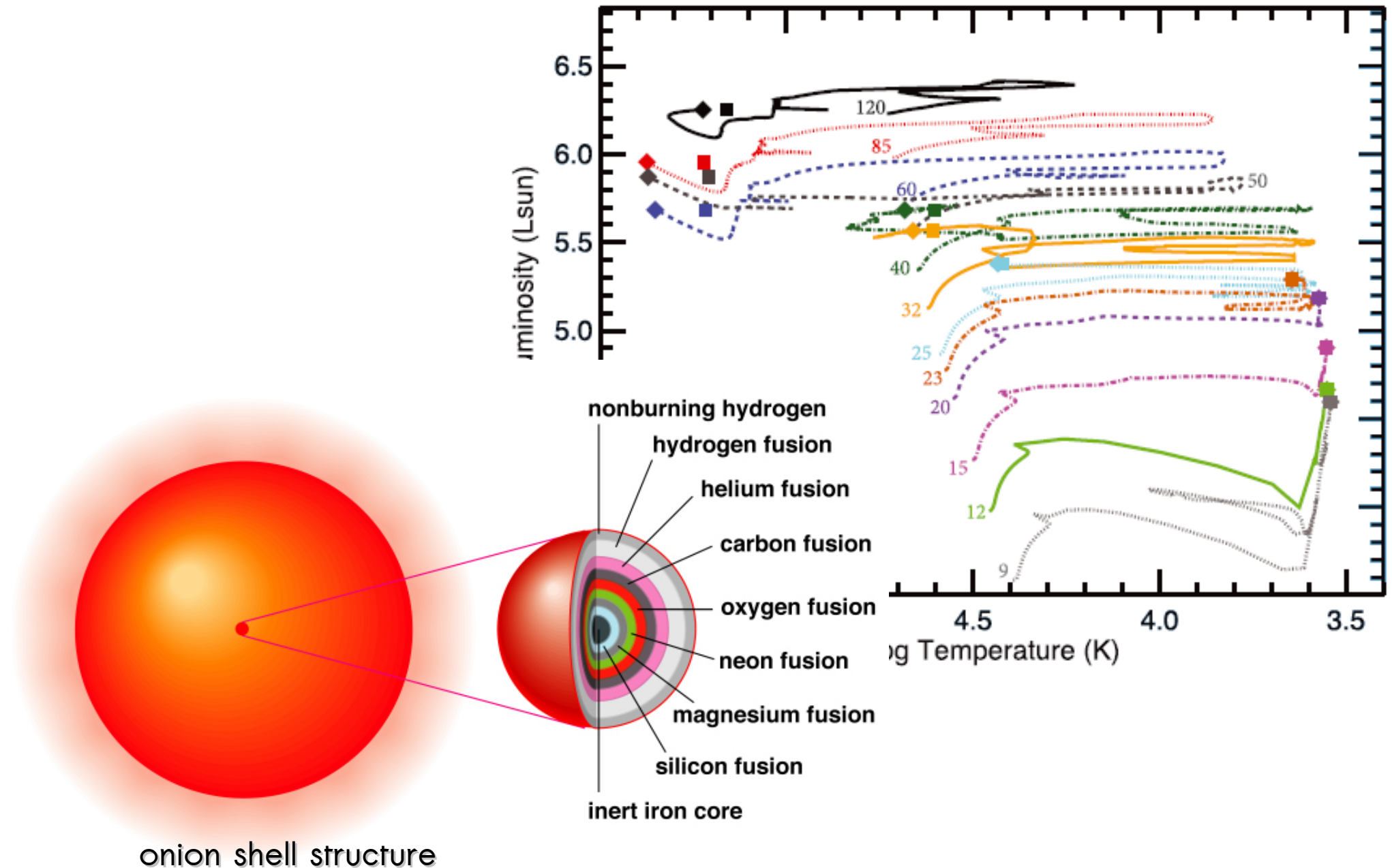
Thermal pulses + global radial pulsations (Mira type)

→ ejection of envelope

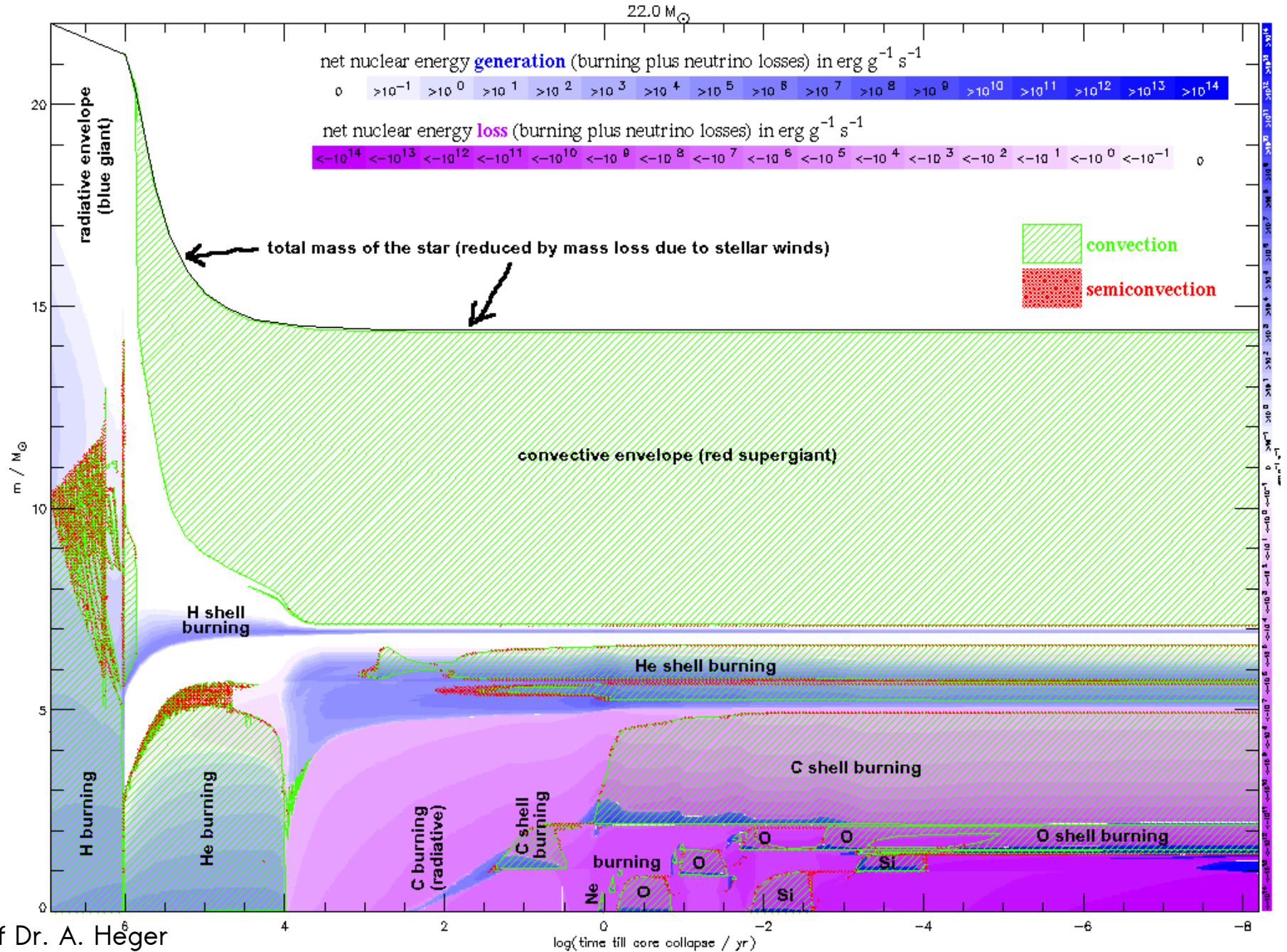
→ potentially a PNae



# Post Main Sequence evolution of massive stars



# Post Main Sequence evolution of massive stars

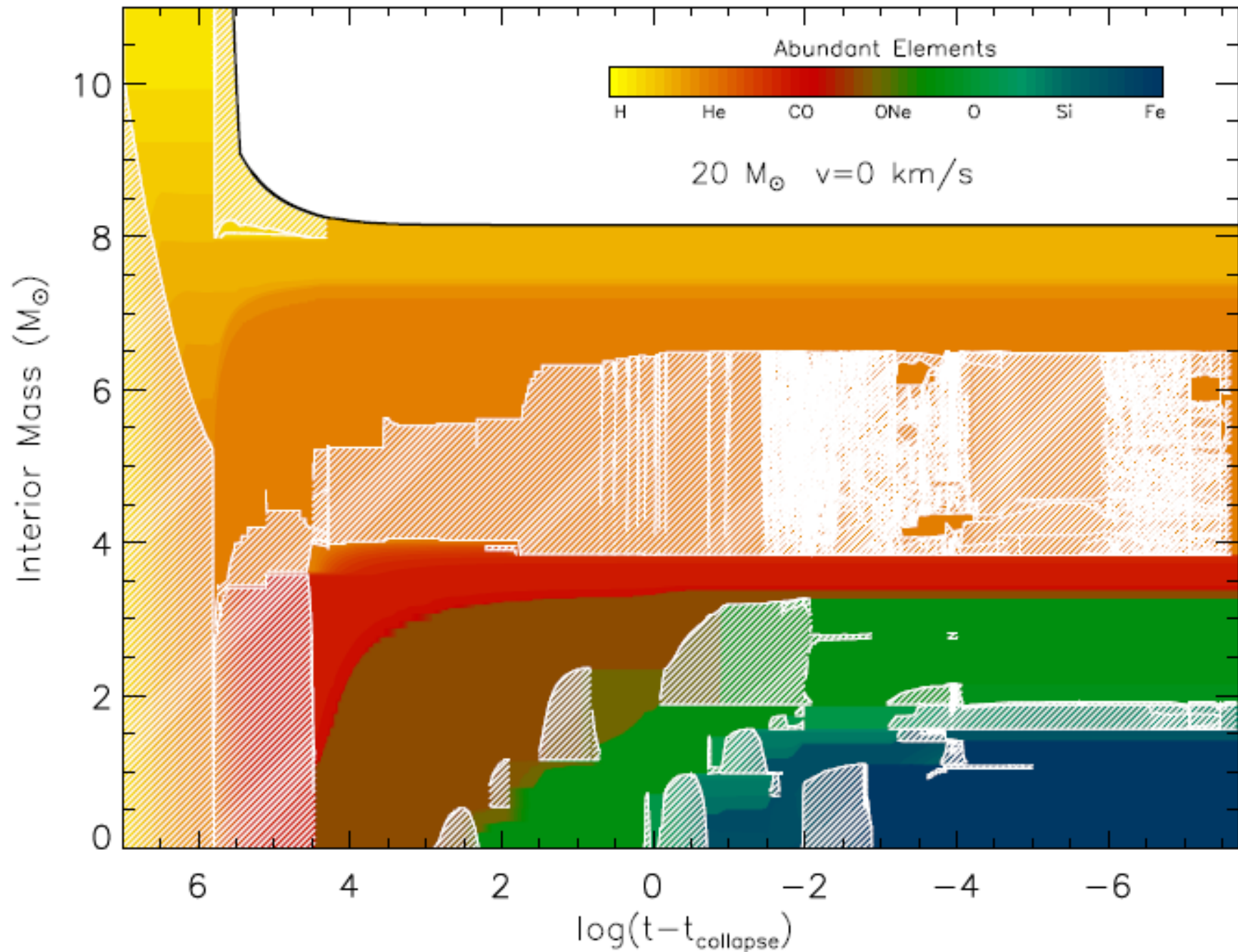


Courtesy of Dr. A. Héger

<http://www.ucolick.org/~alex/stellarevolution/>



# Post Main Sequence evolution of massive stars



# Post Main Sequence evolution of massive stars

## TENTATIVE FILIATIONS:

### **Always blue**

$M > 90 M_{\odot}$ : O – Of – WNL – (WNE) – WCL – WCE – SN (Hypernova ?)

$M > 60-90 M_{\odot}$ : O – Of/WNL  $\leftrightarrow$  LBV – WNL(H poor) – WCL-E – SN (SNIIn?)

$M > 40-60 M_{\odot}$ : O – BSG – LBV  $\leftrightarrow$  WNL – (WNE) – WCL-E – SN (SNIb)  
– WCL-E – WO – SN (SNIc)

### **Blue – red - blue**

$M > 30-40 M_{\odot}$ : O – BSG – RSG – WNE – WCE – SN (SNIb)  
OH/IR  $\leftrightarrow$  LBV ?

### **Blue – red**

$M > 25-30 M_{\odot}$ : O – (BSG) – RSG – BSG  $\leftrightarrow$  RSG SNII  
BLUE LOOP

$M > 10-25 M_{\odot}$ : O – RSG – (Cepheid loop for  $M < 15 M_{\odot}$ ) – RSG – SN SNIIP

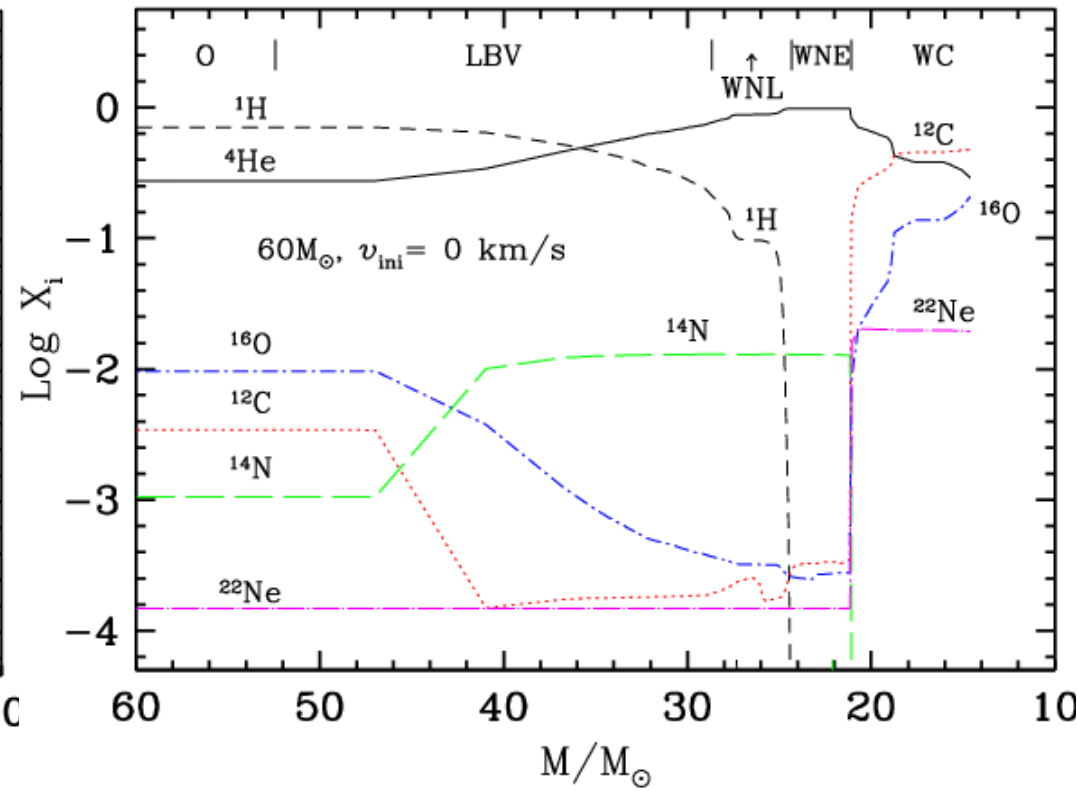
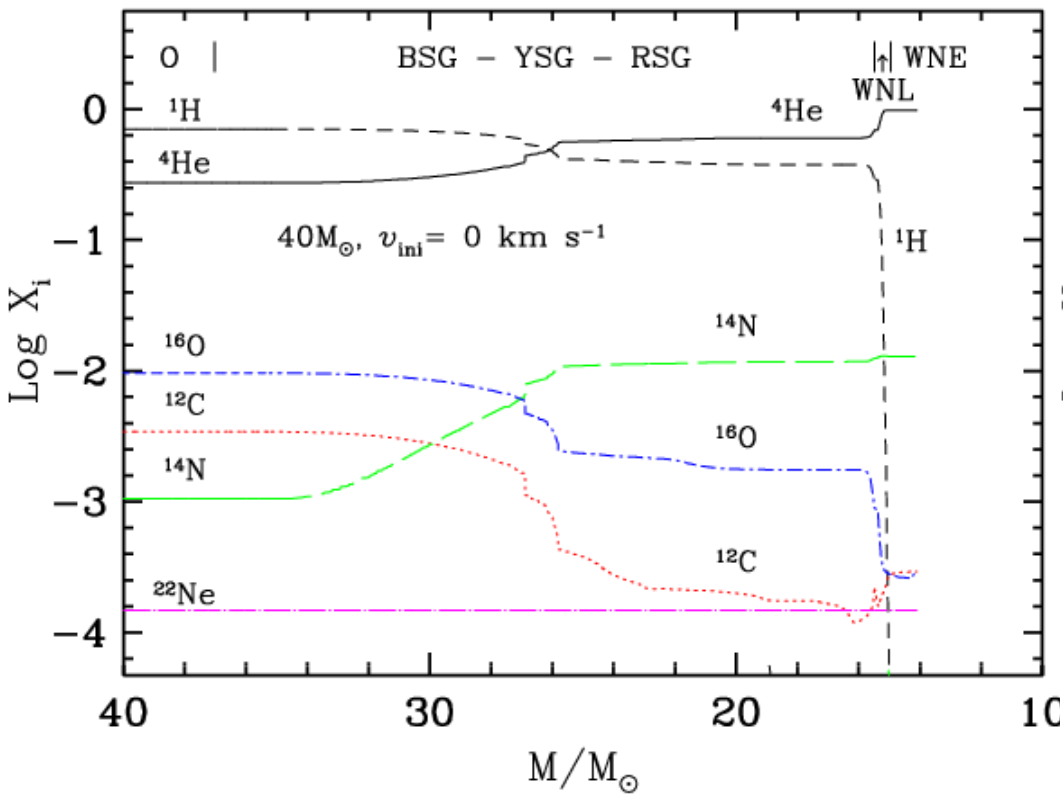
Mass loss driven  
evolution

Normal evolution

This is far from being clear yet!

# Surface abundances evolution for massive stars

O :	BSG à RSG :	WN :	WC:
no expected variation	$^4\text{He} \nearrow$	$^{14}\text{N} \nearrow \nearrow$	$^{14}\text{N} \searrow$
	$^1\text{H} \searrow$	$^{12}\text{C}$ and $^{16}\text{O} \searrow \searrow$	$^{12}\text{C}$ and $^{16}\text{O} \nearrow$
	$^{14}\text{N} \nearrow$	$^{22}\text{Ne}$ and $^{25}\text{Mg} \searrow$	$^{22}\text{Ne} \nearrow \nearrow$

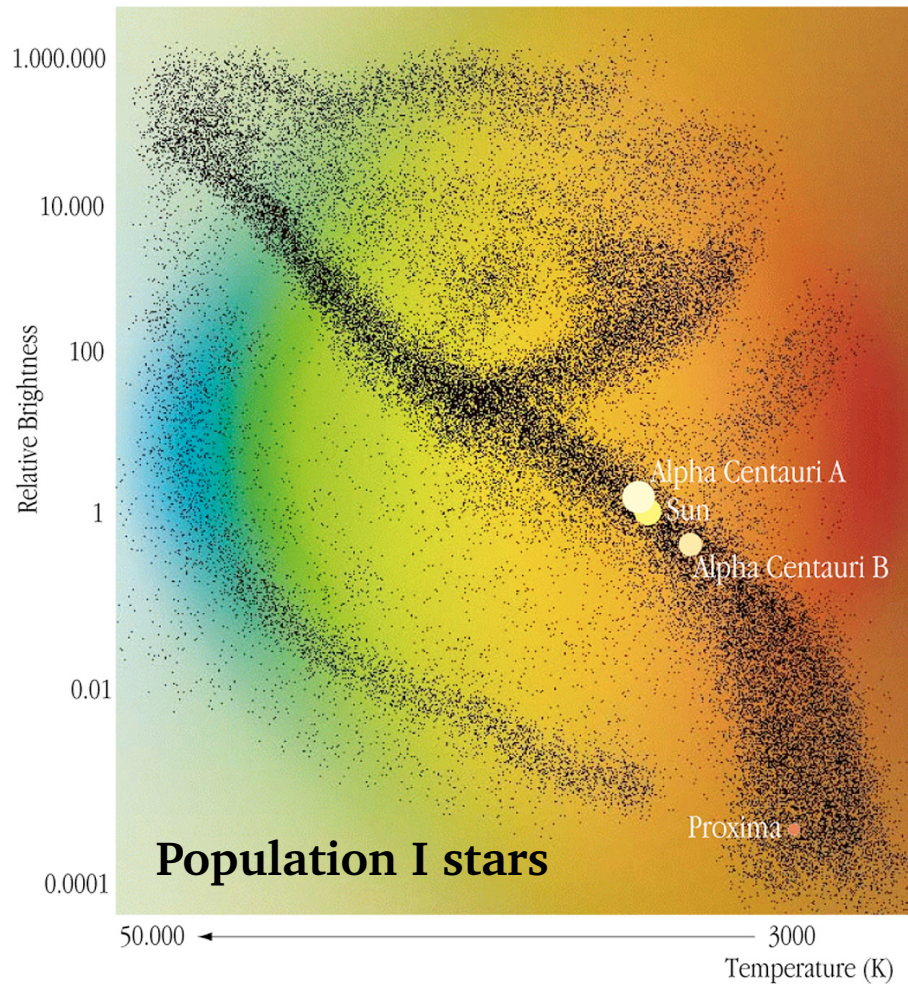




# But there is more to it : lots of challenges!

## A wealth of “abundance anomalies”

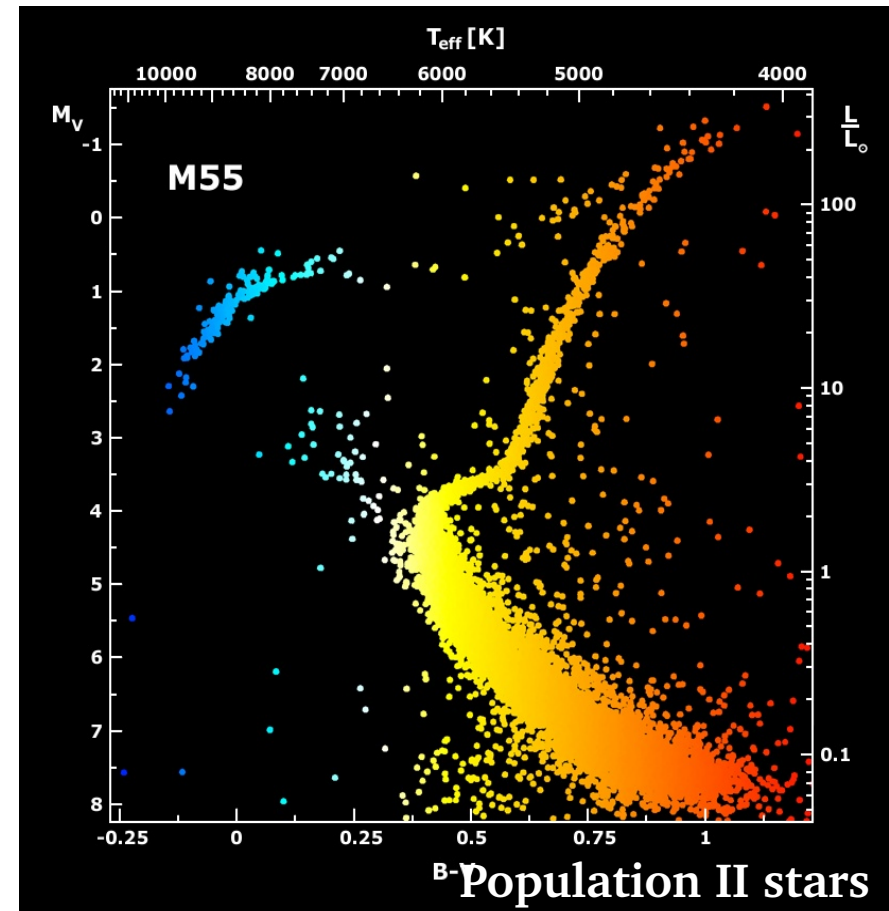
Li anomalies      N and He overabundances      CP stars



Anomalous Fe  
and Fe peak  
elements

Anomalous Li, C, N

Low Li  
Anomalous O, Na,  
Mg, Al

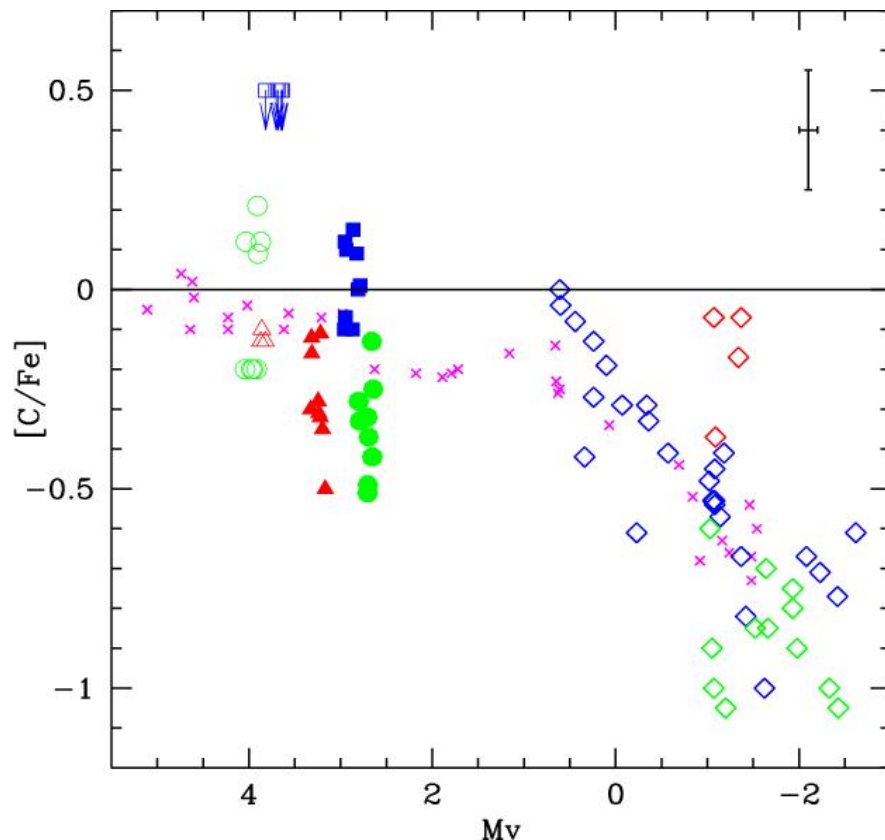




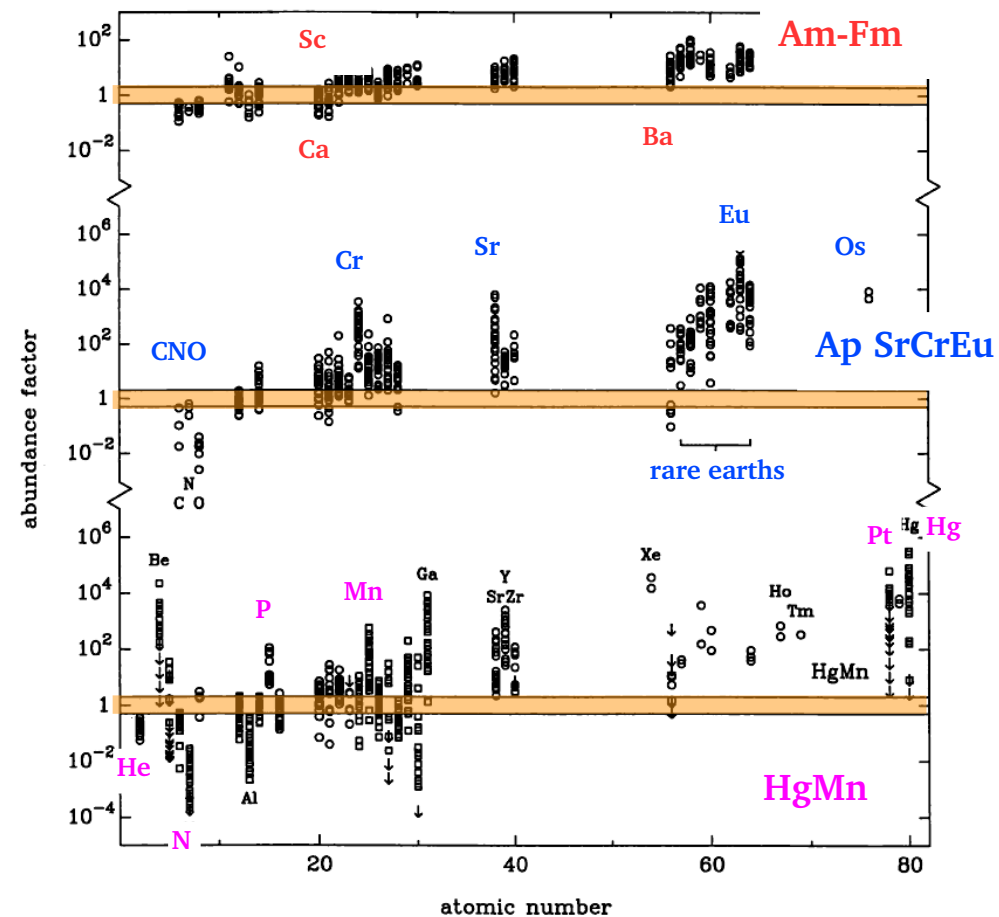
# But there is more to it : lots of challenges!

## A wealth of “abundance anomalies”

Carbon deficiency in evolved red giants of globular clusters



Strong departures from the solar values for the surface abundances of heavy elements in B, A and F type stars

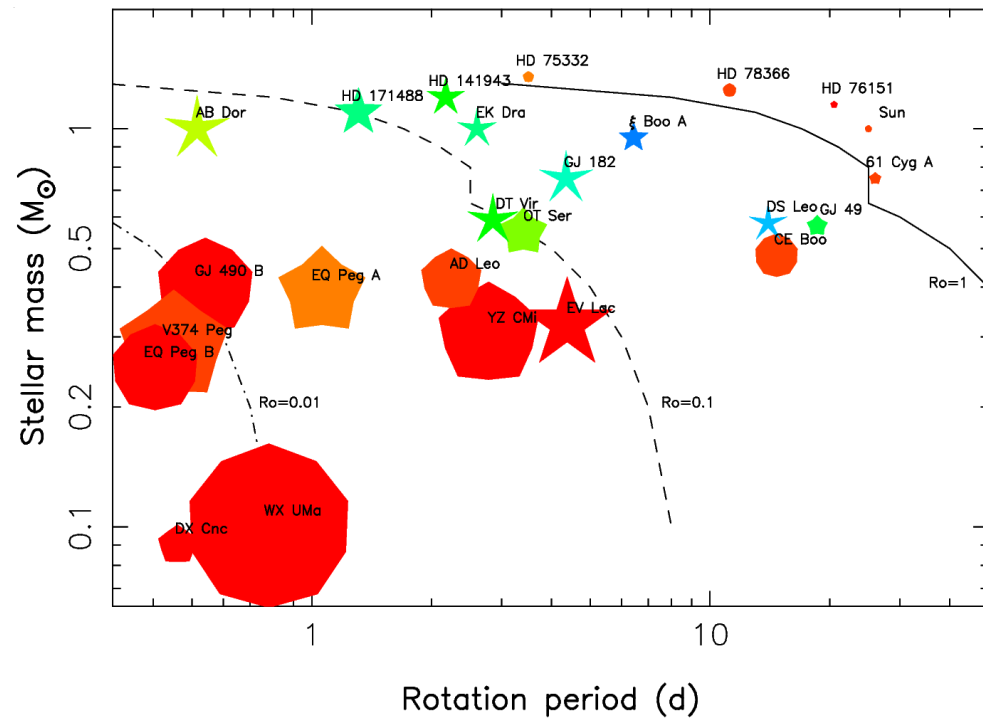


# But there is more to it : lots of challenges!

## Direct evidence of dynamical processes in stars

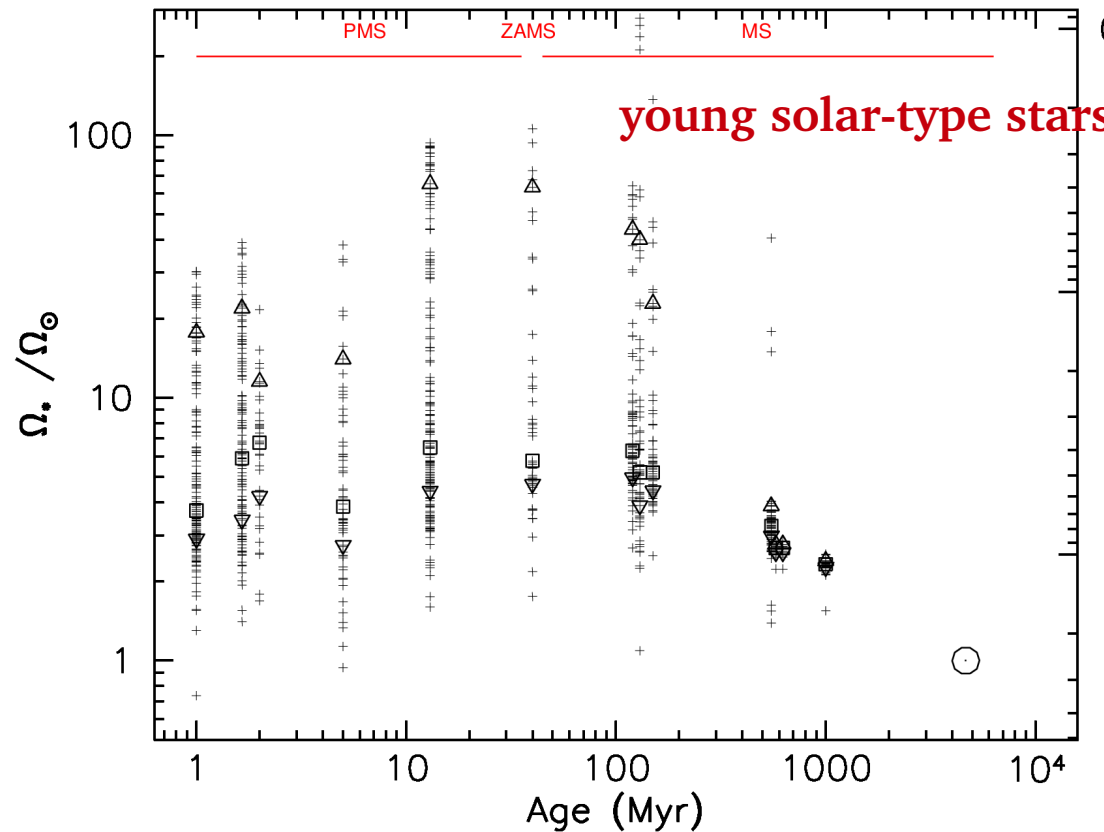
magnetic fields

Donati & Landstreet, 2009



**Low-mass dwarfs**

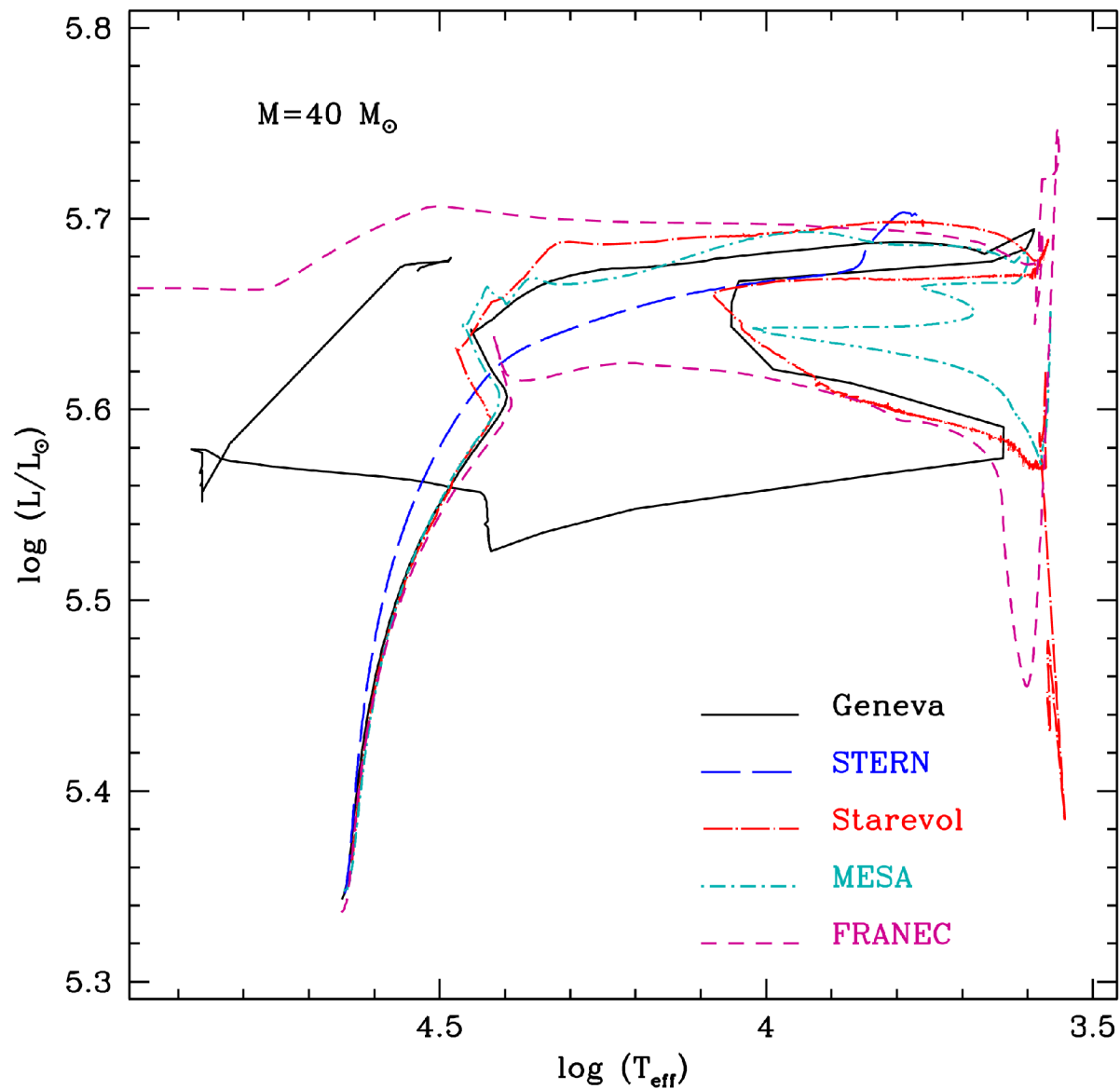
rotation



Gallet & Bouvier 2013

# But there is more to it : lots of challenges!

Mass loss driven evolution ???



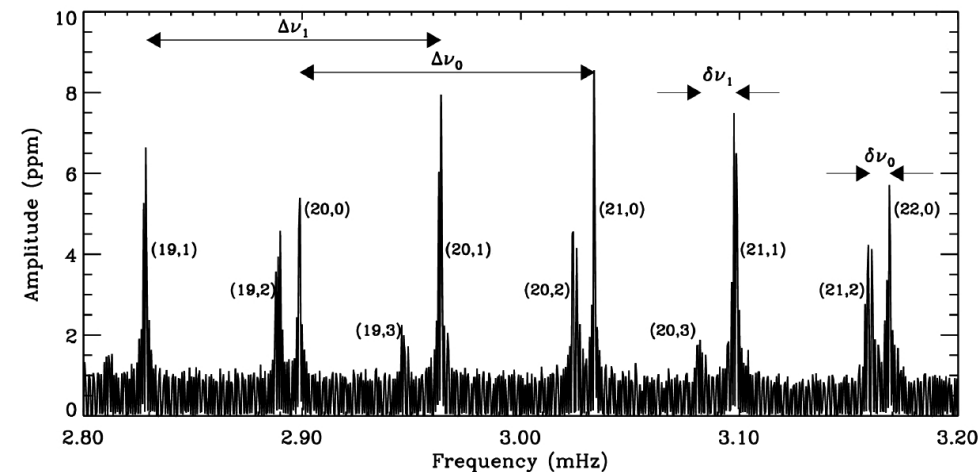
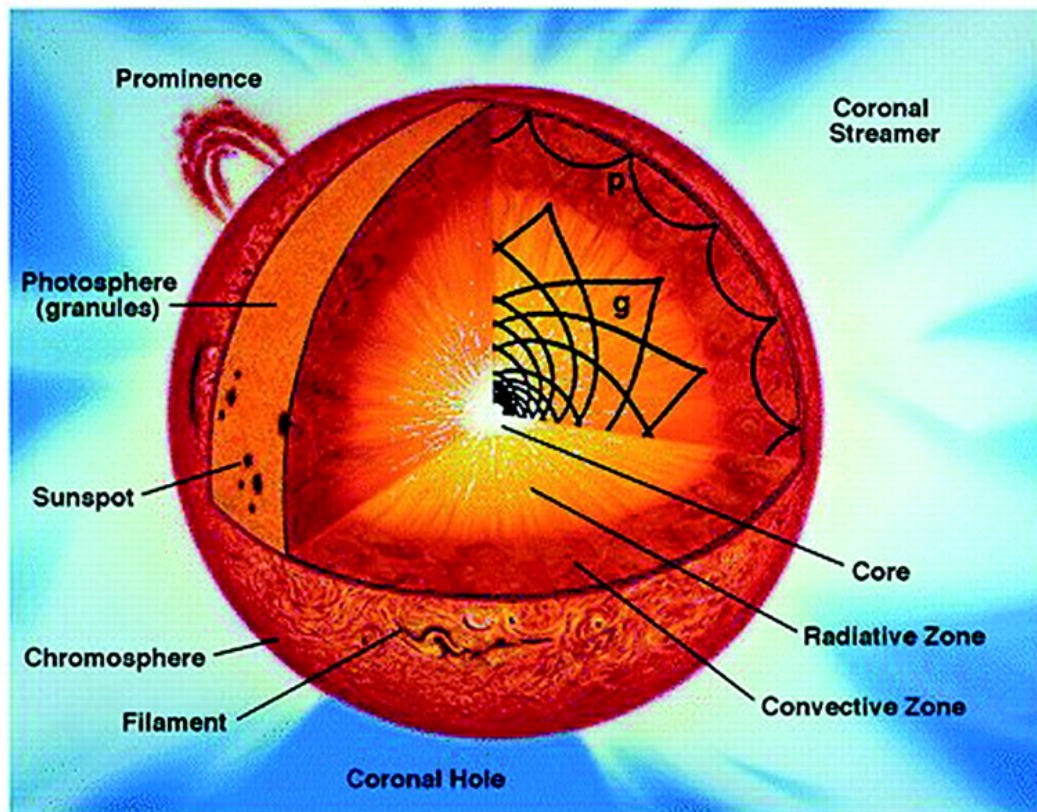
# But there is more to it : lots of challenges!

## Probe stellar structure equations in detail

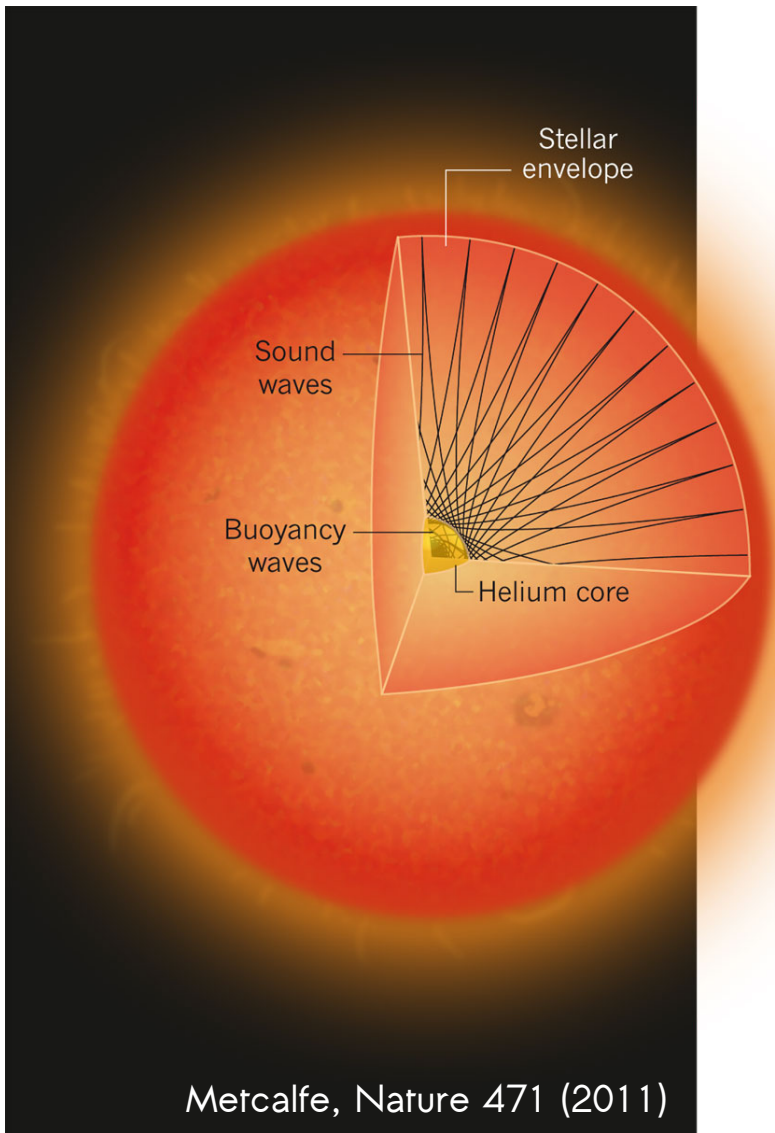
Helioseismology probes the outer 80% of the solar radius via p-modes.

g-modes propagate in the solar core and are not detected in the surface oscillation spectrum.

→ It is extremely difficult to probe the core of the Sun, since only g-mode candidates are found



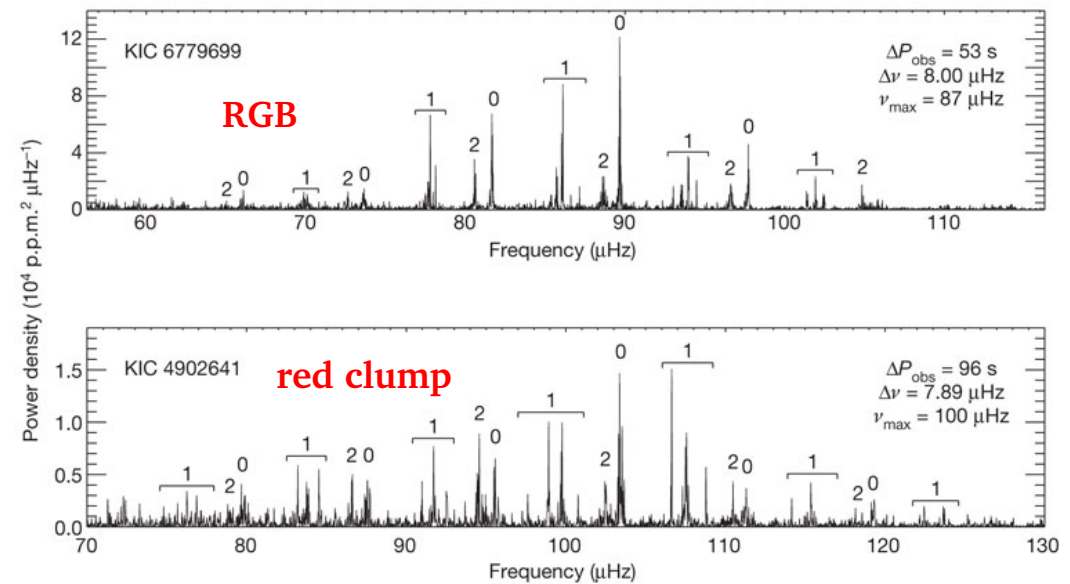
# But there is more to it : lots of challenges!



The solar-like oscillations discovered in red giant stars correspond to p-modes and so-called mixed-modes.

g-modes and p-modes propagate in common cavities

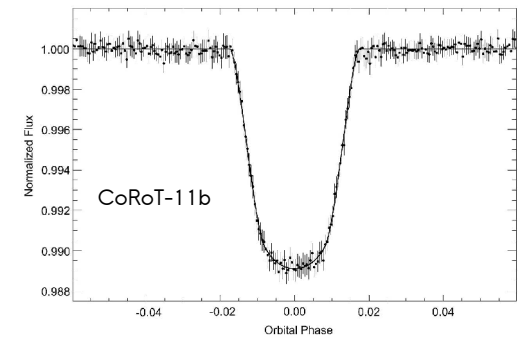
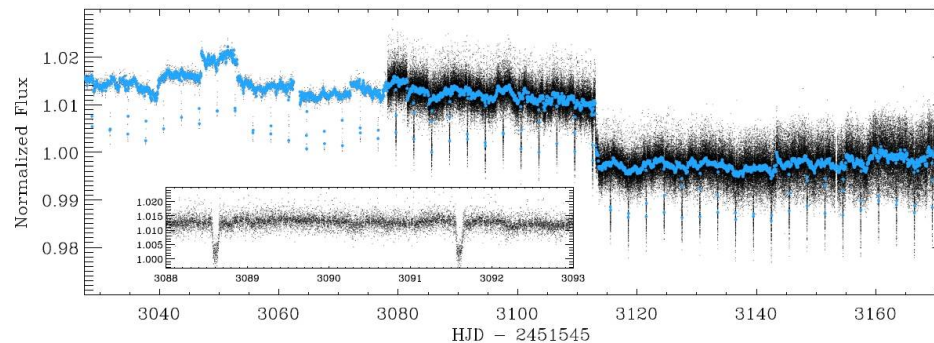
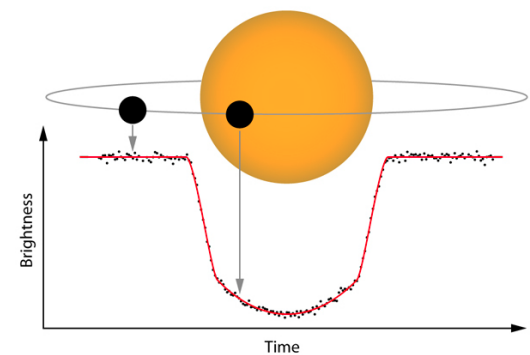
→ they make it possible to probe the core of red giants





# High precision space photometry

High-precision photometry from space + radial velocity follow-up → detection of exoplanetary transits



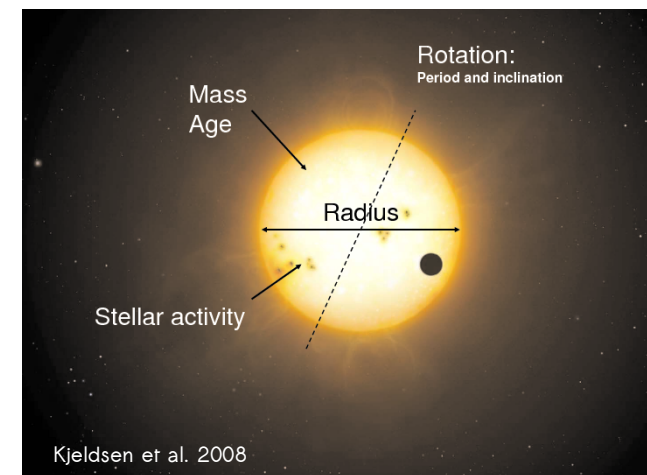
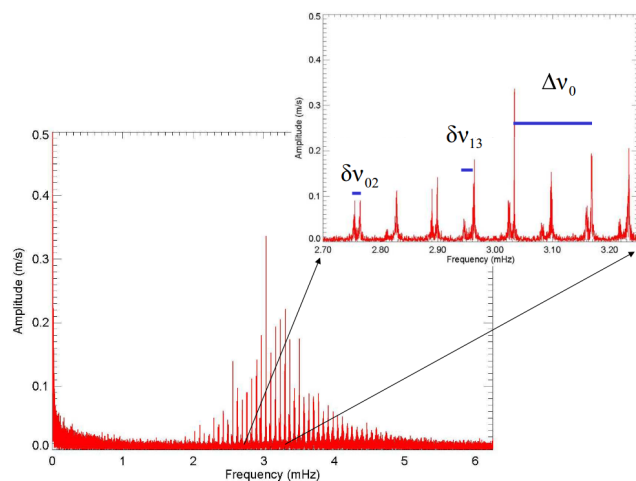
Gandolfi et al., 2010

Fourier analysis of the lightcurves

→ power-spectrum

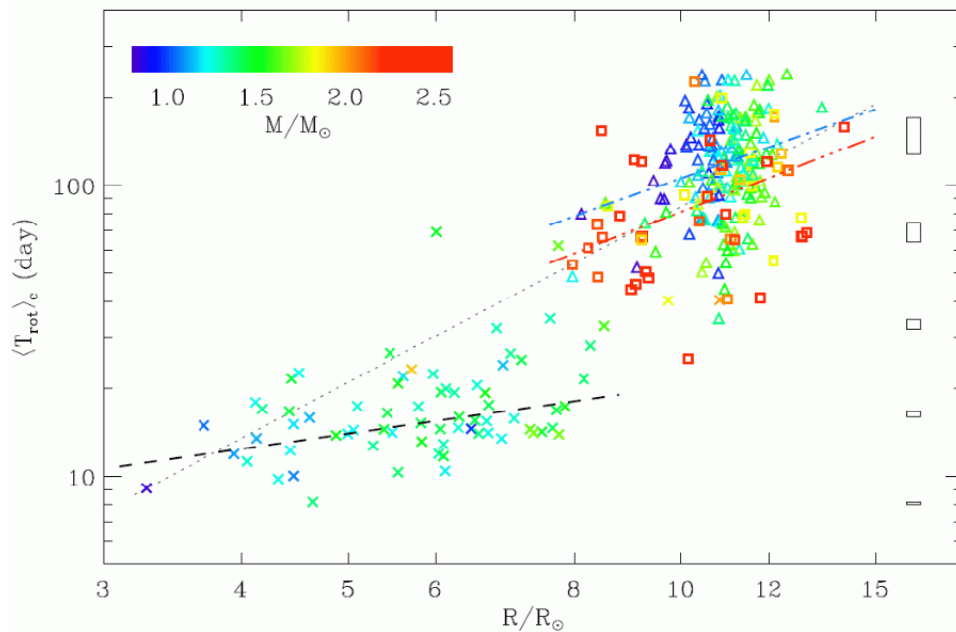
→ asteroseismology

→ probe the internal structure + measure basic properties of stars



# Some results from CoRoT & Kepler

Very successful CoRoT and Kepler missions dedicated to exoplanets detections and asteroseismology



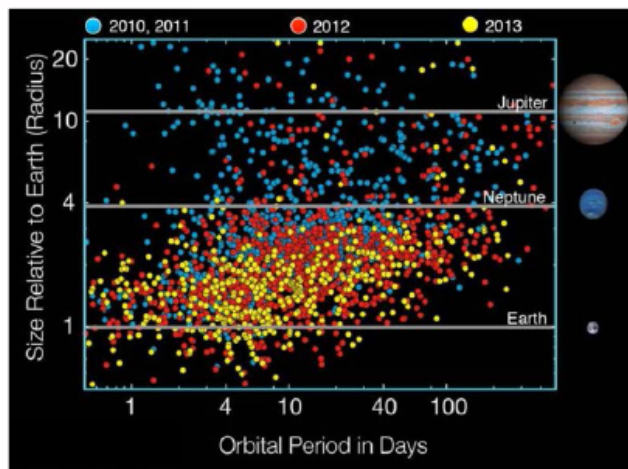
New era for stellar physics

internal rotation of red giants



Large diversity of planetary systems

Kepler planet candidate statistics



CoRoT confirmed exoplanets





# Goal of the PLATO 2.0 mission

## Main goal of PLATO :

detect terrestrial exoplanets in the habitable zone of solar-type stars and characterise their bulk properties

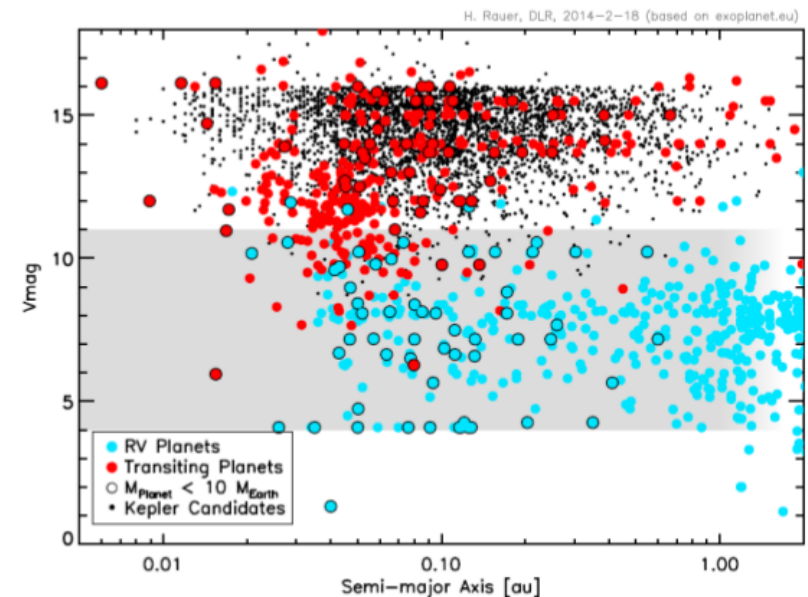
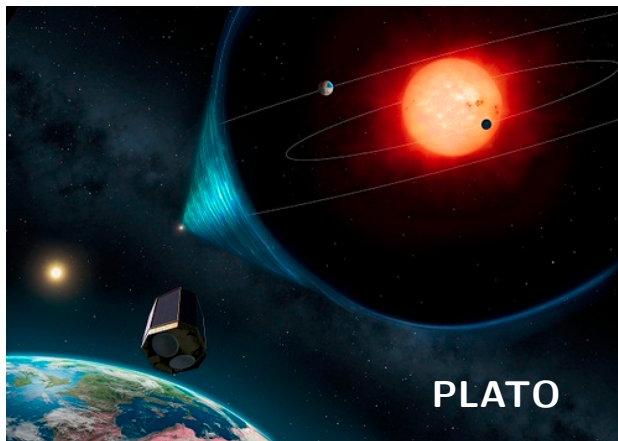
PLATO will be leading this effort by combining:

planet detection and radius determination from photometric transits,

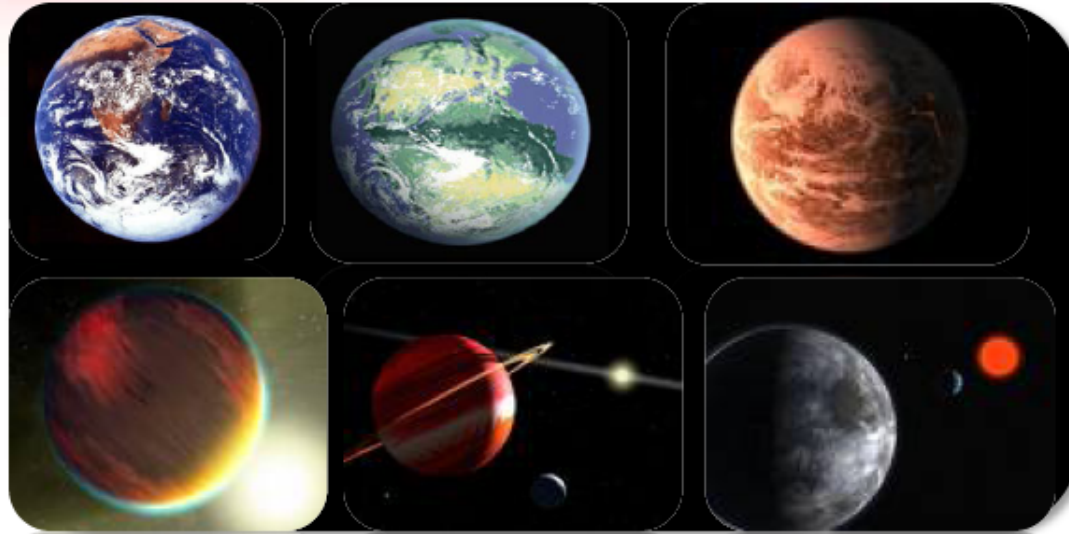
determination of planet masses from ground-based radial velocity follow-up,

determination of accurate stellar masses, radii, and ages from asteroseismology,

identification of bright targets for atmospheric spectroscopy.



# PLATO 2.0: Exoplanets and Stars



Characterization of exoplanets ... needs characterization of stars

- **Mass + radius → mean density**  
(gaseous vs. rocky, composition, structure)
- **Orbital distance, atmosphere**  
(habitability)
- **Age**  
(planet and planetary system evolution)
- **Stellar mass, radius**  
(derive planet mass, radius)
- **Stellar type, luminosity, activity**  
(planet insolation)
- **Stellar age**  
(defines planet age)

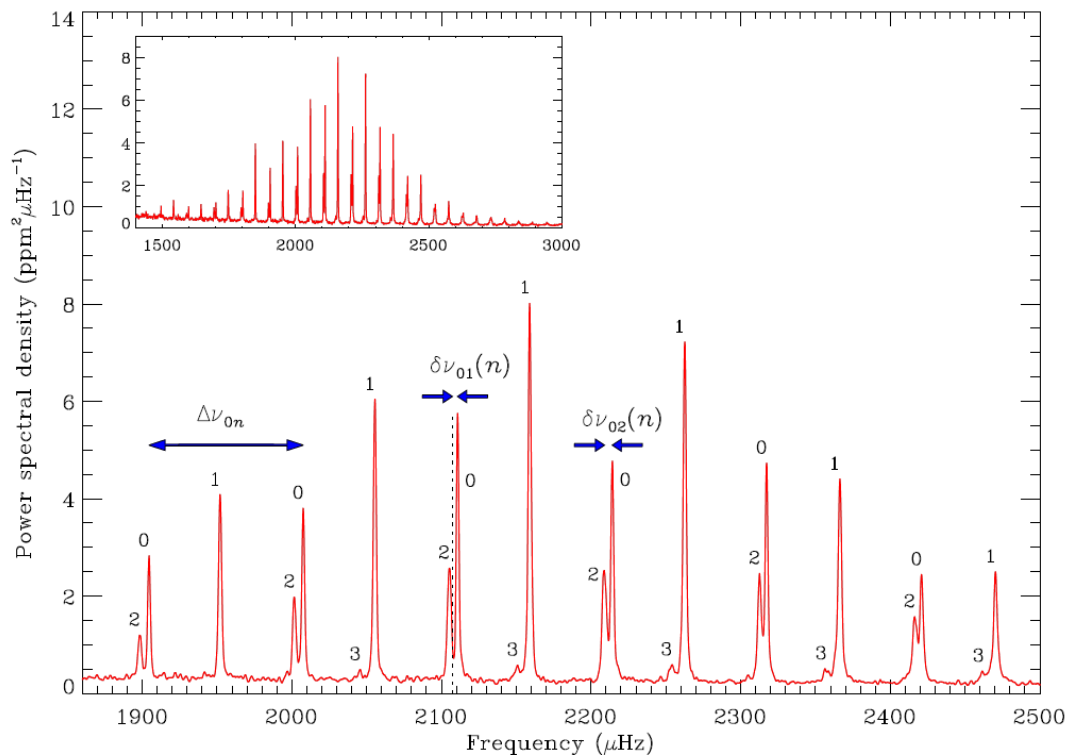
# Stellar modelling for asteroseismology

Oscillation spectra computed from stellar models guide the identification of modes.

The separations between modes allow to retrieve  $M$  and  $R$  provided that  $T_{\text{eff}}$  is well known

→ need to combine high precision photometry and **spectroscopy**

→ need a grid of precise **stellar models** to interpret oscillation spectra



$$\frac{\Delta\nu}{\Delta\nu_{\odot}} = \left(\frac{M}{M_{\odot}}\right)^{0.5} \left(\frac{R}{R_{\odot}}\right)^{-1.5}$$

$$\frac{\nu_{max}}{\nu_{max,\odot}} = \left(\frac{M}{M_{\odot}}\right) \left(\frac{R}{R_{\odot}}\right)^{-2} \left(\frac{T_{eff}}{T_{eff,\odot}}\right)^{-0.5}$$

$$\delta\nu \propto \frac{dc_s}{dr} \rightarrow \text{age dependent}$$

PLATO shall give

$M$  within 2%

age within 10 %